

# **Data Assimilation Technique Development in and related to the Warn-on-Forecast Project**

Warn-on-Forecast Workshop

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Norman Oklahoma

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## Data Assimilation Tools in WoF Toolbox

- WRF DART (for WRF and NCOMMAS)
- ARPS EnKF System (for ARPS and WRF)
- ARPS 3DVAR/Cloud Analysis
- WRF 3DVAR and 3DVAR-Hybrid
- GSI-based EnKF/EnKF-Hybrid (for WRF and others)

# DA Technique Development in WoF

- CAPS's multi-scale parallel EnKF system
  - Hybrid OpenMP/MPI parallelization
  - Multiple data types, especially high-density radar data
  - 4D asynchronous filter (4DEnSRF), and iterative procedure (iEnSRF) for faster convergence/spin up
  - Interface with both ARPS and WRF
  - Support for 2-moment microphysics, perturbed physics and multi-physics ensemble, build-in attenuation correction
  - Microphysical parameter estimation
  - Polarimetric radar data assimilation
  - Adaptive covariance inflation, successive spatial localization
  - EnKF-3DVAR hybrid and LETKF algorithms (under development)
  - En4DVAR (planned)

# DA Technique Development in WoF

- Enhancements to ARPS 3DVAR/Cloud Analysis System
  - Added diagnostic pressure equation constraint
  - Direct assimilation of reflectivity data with hydrometeor classification
  - Vertical correlation scale defined in terms of height
  - 2-moment MP scheme support and use of dual-pol data in cloud analysis (under development)
- WRF 3DVAR/Hybrid System
  - Applied to radar radial velocity assimilation of a hurricane case
- GSI-based EnKF and EnKF-Hybrid
  - Tested for Rapid Refresh configurations including all operational data at a 40 km grid spacing,
  - Developed dual-resolution capabilities for EnKF
  - One-way and two-interactive EnKF-Hybrid

# Posters on EnKF Algorithms (algorithm development)

- 14) Doppler Radar Data Assimilation using a Local Ensemble Transform Kalman Filter (**LETKF**, Therese Thompson)
- 22) Implementation of **LETKF** with ARPS model and some preliminary results of OSSE (Gang Zhao)
- 19) **Multi-scale EnKF** data assimilation and forecasts of the 10 May 2010 tornado case in the central US domain (Youngsun Jung)
- 20) A four-dimensional asynchronous ensemble square-root filter (**4DEnSRF**) algorithm and tests with the 10 May 2010 tornado case (Shizhang Wang)

# Posters on EnKF Analyses Coupled with Multi-moment Microphysics

- 7) The Impact of Single and Double Moment Microphysics Schemes on Ensemble Kalman Filter Analyses and Forecasts of the 8 May 2003 Tornadic Supercell Storm (Nusrat Yussouf)
- 10) Multi-Moment and Multi-Phase Ice Microphysics in Storm-scale EnKF (Ted Mansell)
- 15) Ensemble prediction of the 4 May 2007 Greensburg, KS tornadic supercell: Impact of microphysics (Daniel Dawson)
- 21) The analysis and prediction of microphysical states and polarimetric variables in a mesoscale convective system using double-moment microphysics, multi-network radar data, and the ensemble Kalman filter (Bryan Putnam)

# Posters on GSI-based EnKF/Hybrid, 3DVAR Analysis of Reflectivity, etc.

- 23) GSI-based EnKF and EnKF-hybrid development and testing for Rapid Refresh configurations (Kefeng Zhu et al.)
- 24) The impact of covariance inflation methods on the spread of ensemble simulations (Tim Supinie)
- 25) Assimilation of attenuated data from an X-band radar network for a quasi-linear storm using the ensemble Kalman filter (Jing Cheng)
- 6) Assimilation of reflectivity data in a convective-scale, cycled 3DVAR framework with hydrometeor classification (Jidong Gao)

# An Iterative Ensemble Square Root Filter (iEnSRF)

- Use radar data multiple times at the beginning of assimilation cycles when state estimation and ensemble covariance are poor.
- Serve to accelerate filter convergence/storm spin up
- Similar to ‘Running-in-Place’ idea for LETKF (Kalnay and Yang 2010)
- Tests with Simulated Radar Data for Storm Scale Data Assimilation

Wang et al. (2012 QJ)

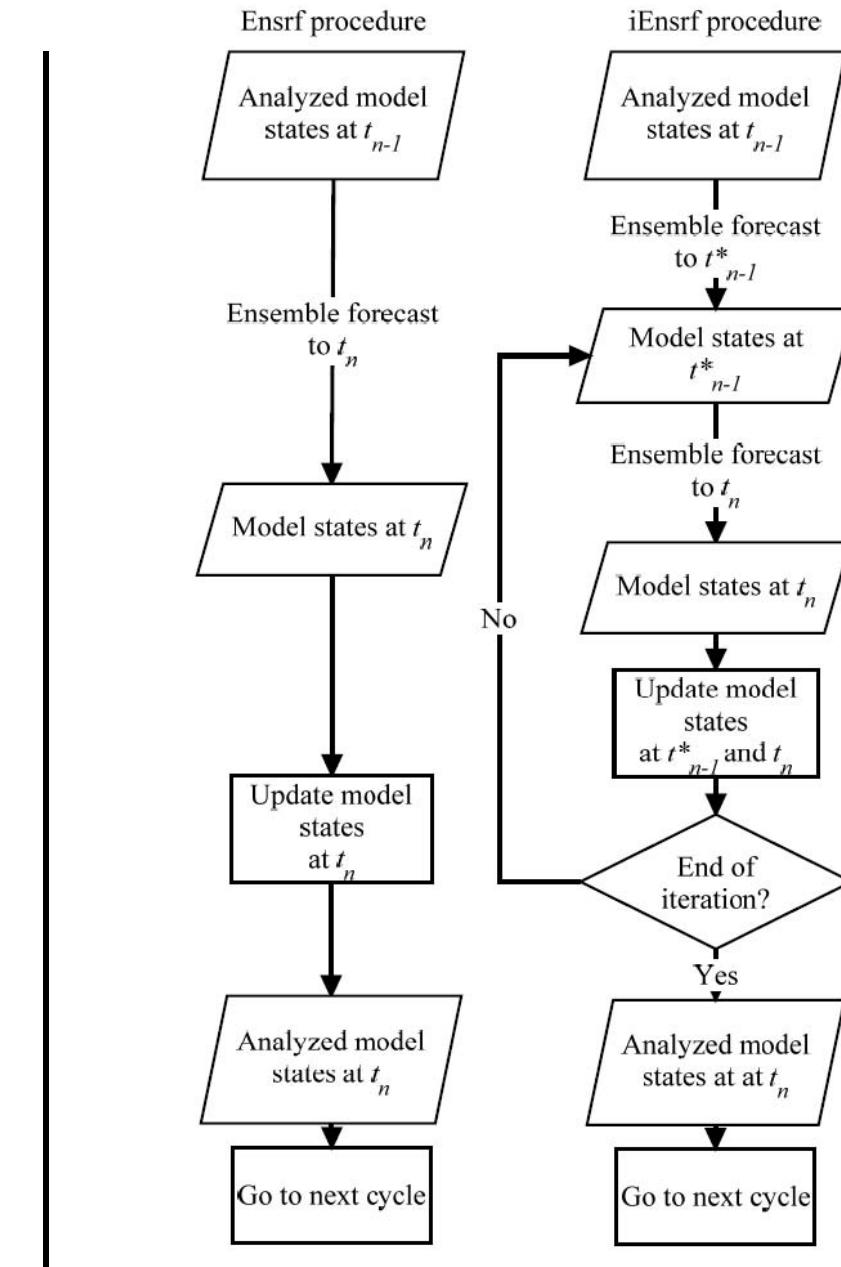


Figure 1. The Flow chart for EnSRF and iEnSRF procedure in each cycle, where the  $t^*_{n-1}$  is an arbitrarily intermediate time between  $t_{n-1}$  and  $t_n$ .

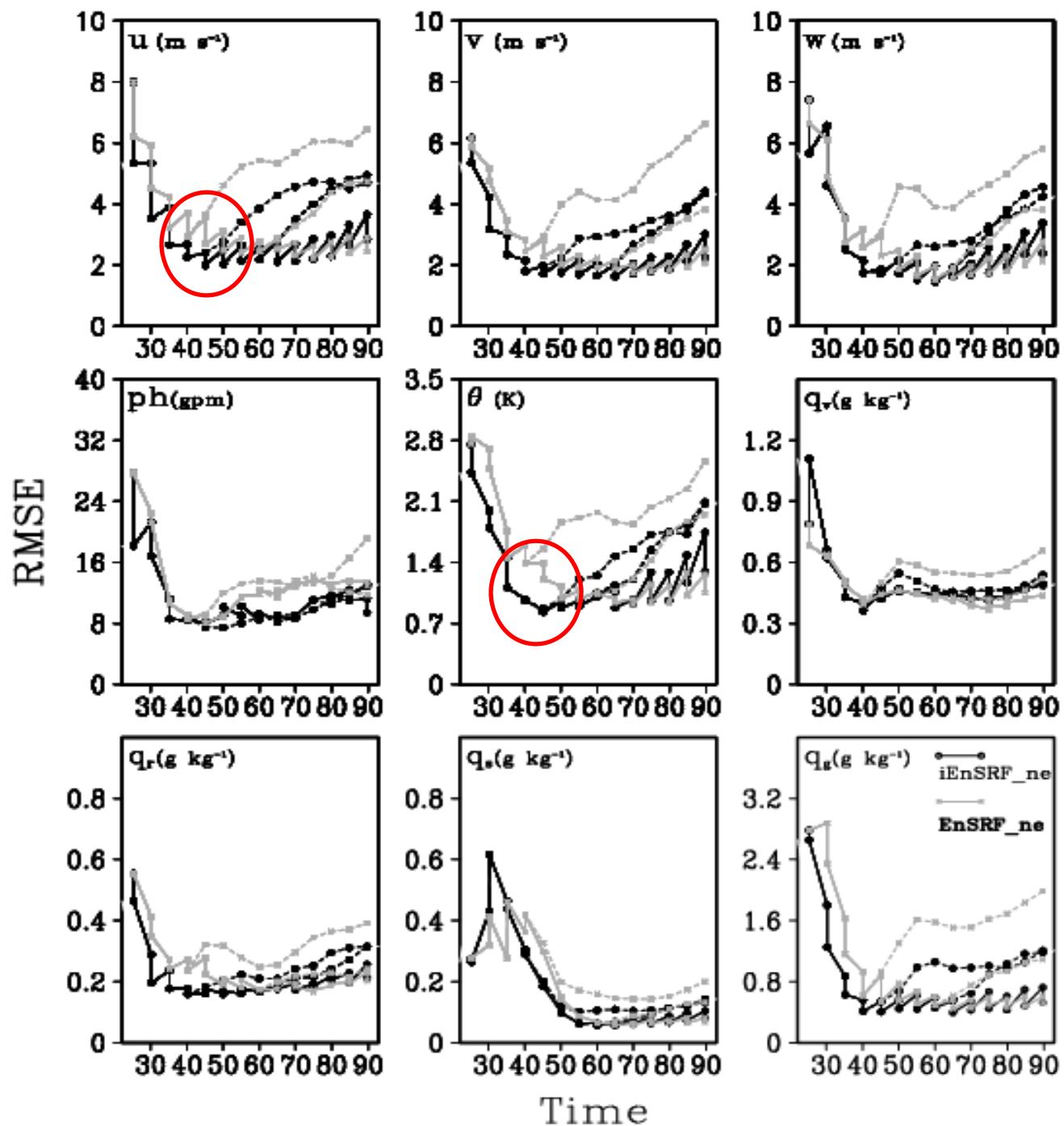
# Supercell OSSE Tests with WRF

Analysis and Forecast Errors

Gray: EnSRF

Black: iEnSRF

Free forecasts  
launched after 4  
analysis cycles



# 4D Asynchronous EnSRF (4DEnSRF)

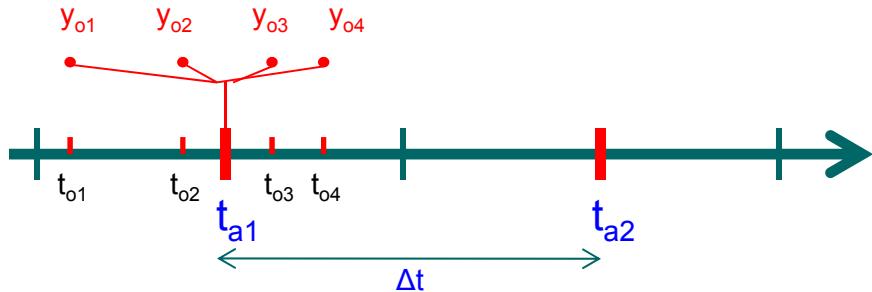
- Motivation
  - High-frequency EnKF DA is costly, given that data I/O can cost >80% overall (reading and writing of ensembles).
  - 4D extension of EnKF requires fewer cycles while still using obs at their correct times
  - Implemented based on the serial EnSRF algorithm in the ARPS EnKF framework – 4DEnSRF

Poster 20: (Shizhang Wang)

Wang, Xue and Min (2012)

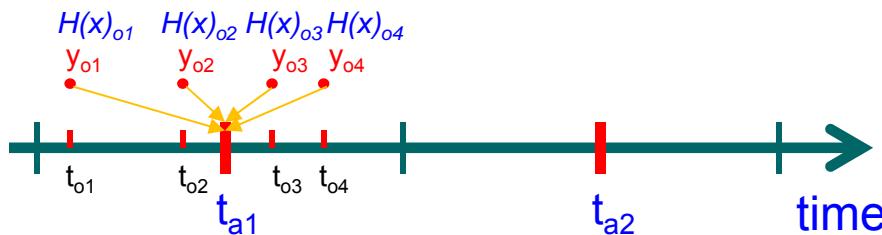
# 4DEnKF vs. Regular EnKF

**EnKF:** Observation are assumed to be taken at the assimilation time, like 3DVAR.



$t_a$ : time of analysis,       $\Delta t$ : analysis time interval,  
 $t_o$ : time of observation

**4DEnKF:** Observation can be assimilated at the times they are taken – no timing error, like 4DVAR

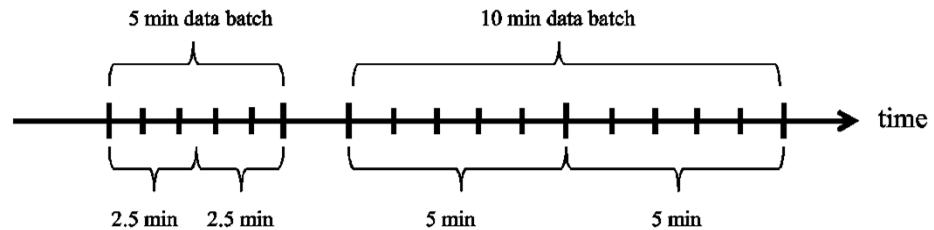


$H(x)$  can be calculated within the numerical model – added to ARPS.

- Existing 4D ensemble algorithms include 4D-LETKF, En4DVAR.
- 4D EnSRF algorithm requires special treatment due to its serial nature.
- 4DEnSRF computes and update observation priors at the observations times.
- 4DEnSRF has been tested with simulated radar data for both WRF and ARPS, and with real data and ARPS.

# Asynchronous EnSRF (AEnSRF) assimilation of radar data OSSE with WRF

- Following Sakov et al (2010), an asynchronous ensemble square-root filter (AEnSRF) has been developed in the WRF framework.
- The performance of AEnSRF and EnSRF for radar DA is tested with OSSEs



Radar observations are grouped into batches with different time spans (5 min and 10 min).

## Performance evaluation

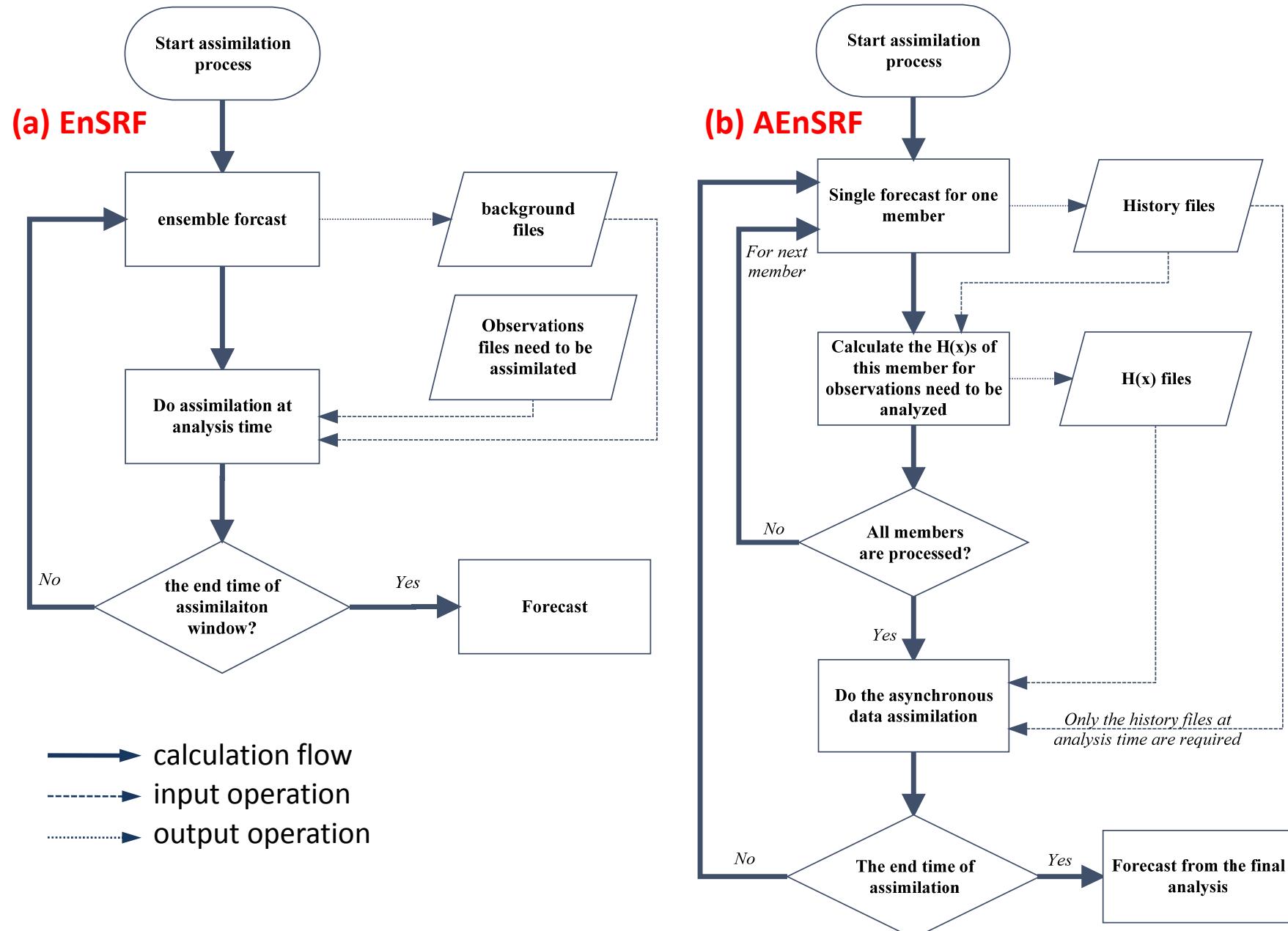
- Difference Total Energy (DTE) (Meng and Zhang 2007)

$$DTE = 0.5(u'u' + v'v' + w'w' + kT'T')$$

- HydroDTE for variables associated with water

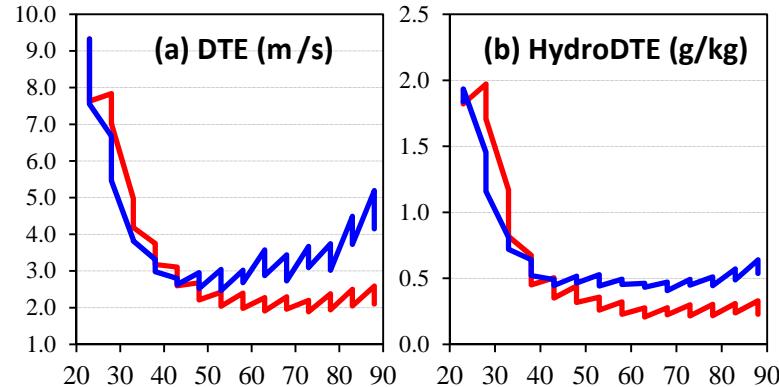
$$HydroDTE = 0.5(q_v'q_v' + q_r'q_r' + q_s'q_s' + q_g'q_g')$$

# Process Flowchart of AEnSRF and EnSRF

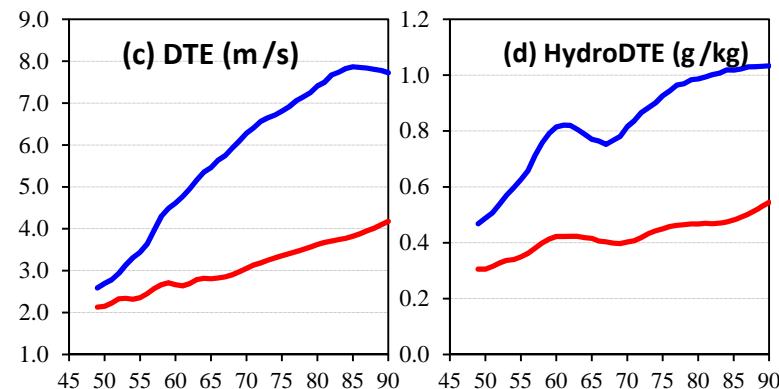


# EnSRF and 4DEnSRF Analysis and Forecast Errors: OSSEs for a Supercell with WRF

Blue: EnSRF   Red: 4DEnSRF

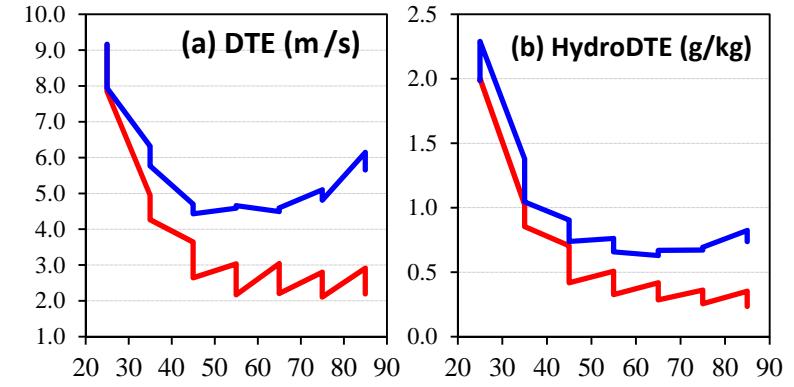


during  
analysis

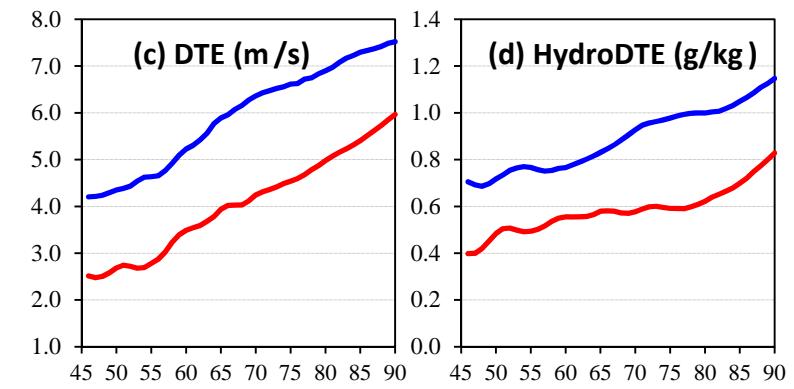


during  
forecast

**5 min data batch**

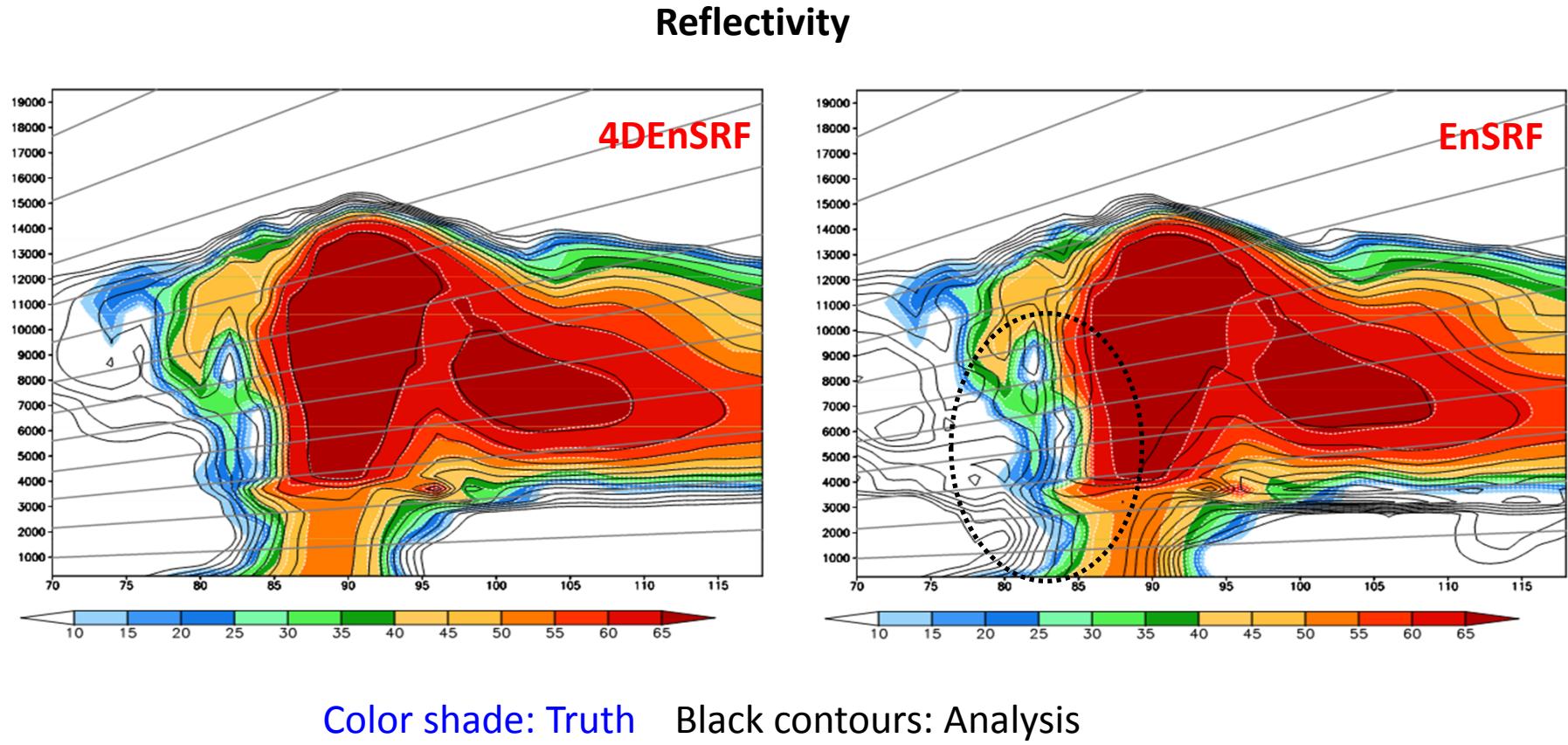


**10 min data batch**



- The RMS errors of 4DEnSRF are lower than those of EnSRF.
- The advantage of 4DEnSRF is more when analysis interval is longer (10 min or longer).
- Forecast error with 4DEnSRF grow faster for 10 min data batches than the 5 min case, while the growth rates for EnSRF are fast in both cases.

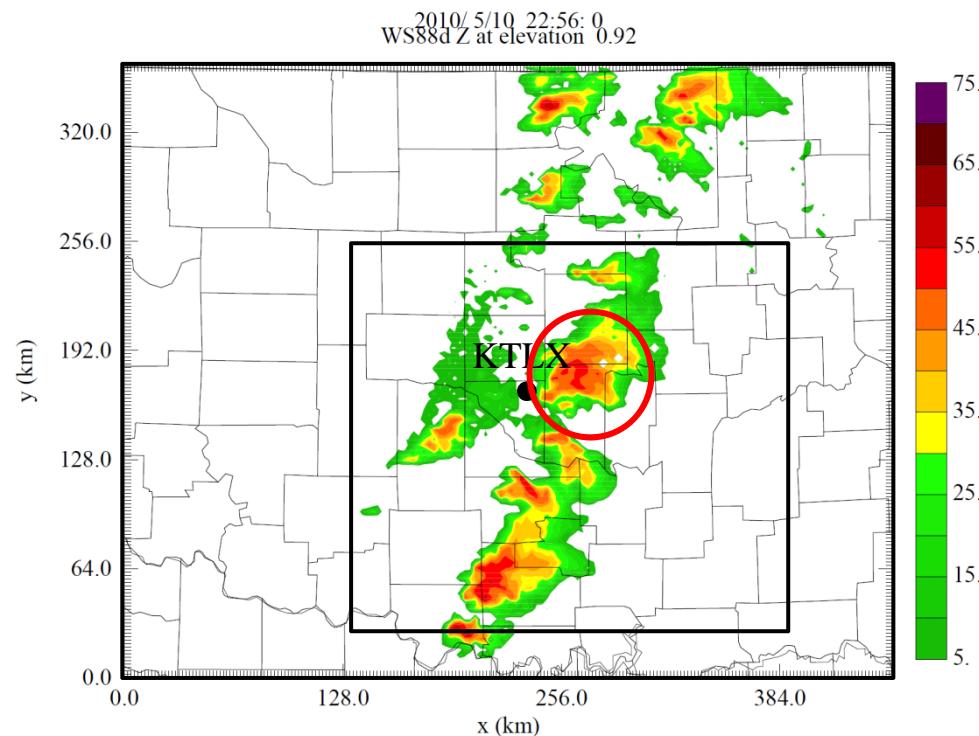
## 4DEnSRF v.s. EnSRF with 5 min data batches



- Analyzed reflectivity with EnSRF exhibits larger errors due to timing error

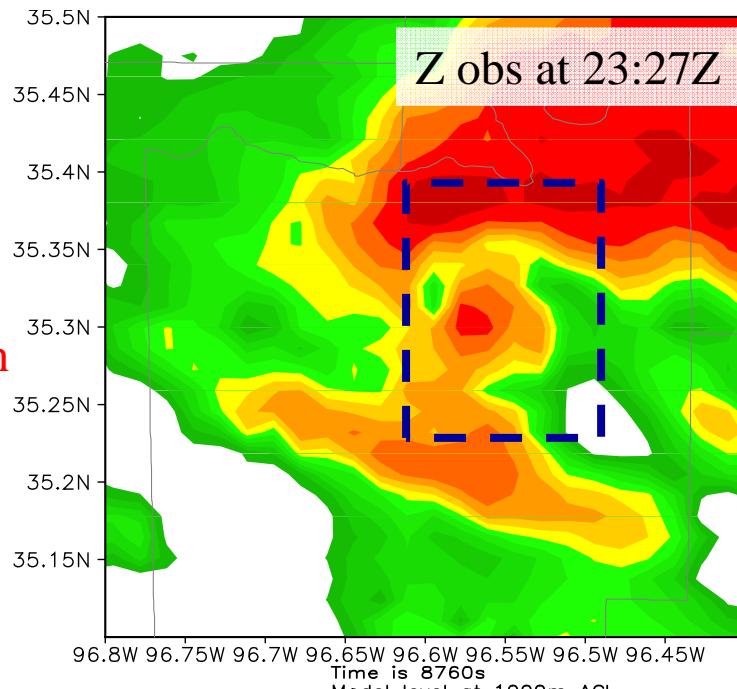
- Analysis of a tornadic supercell on May 10, 2010
- EnSRF v.s. 4DEnSRF

1.5 km grid  
nested within  
a 3 km grid

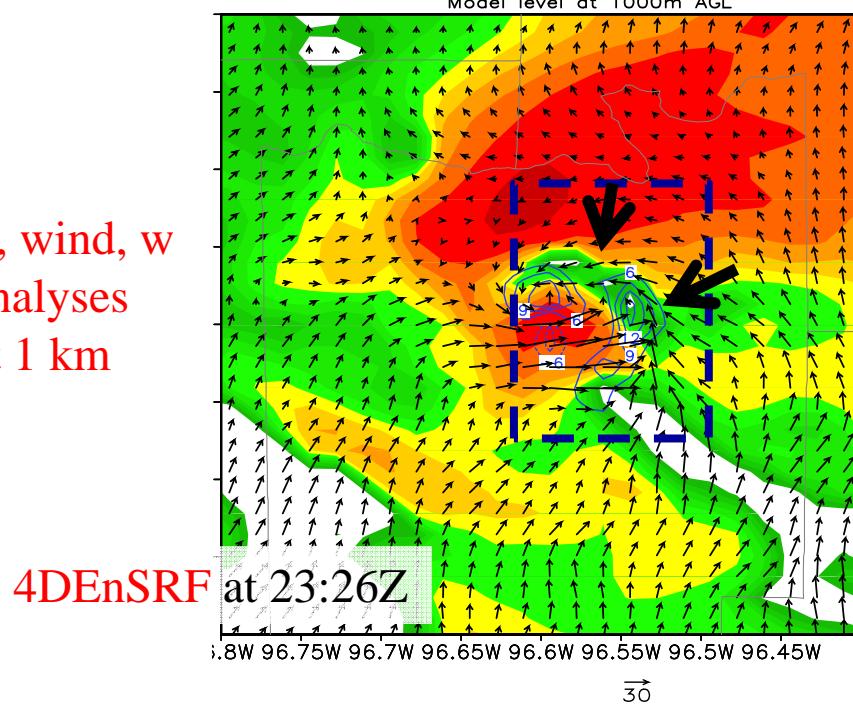


(See Poster 20)

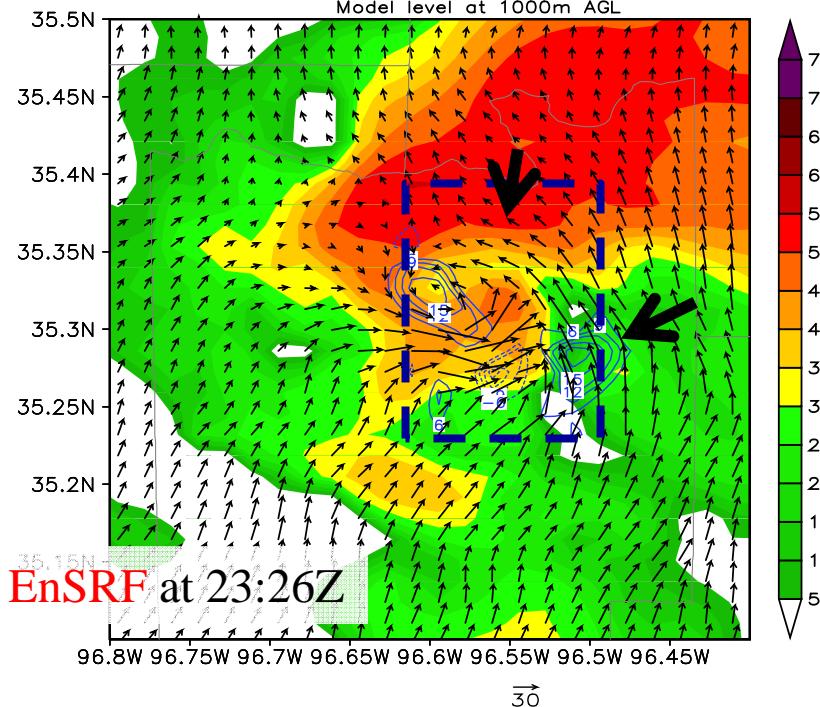
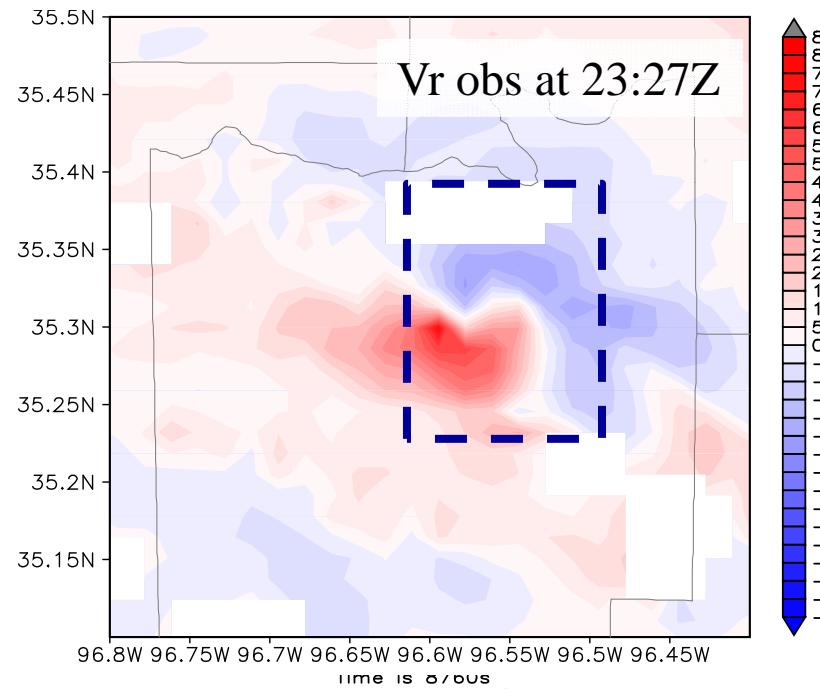
OBS  
at 0.52°  
Elevation



Z, wind, w  
analyses  
at 1 km



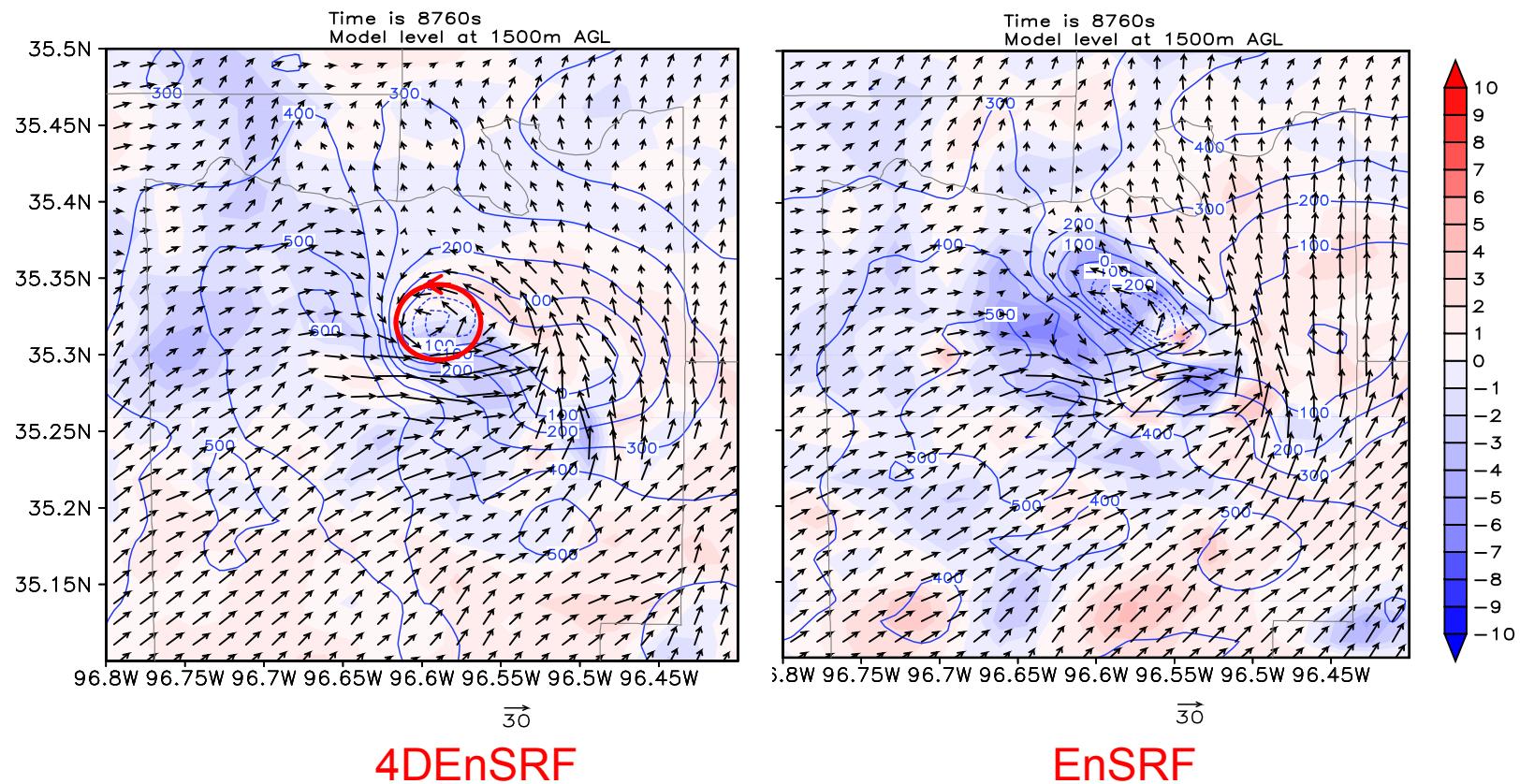
4DEnSRF  
at 23:26Z



30

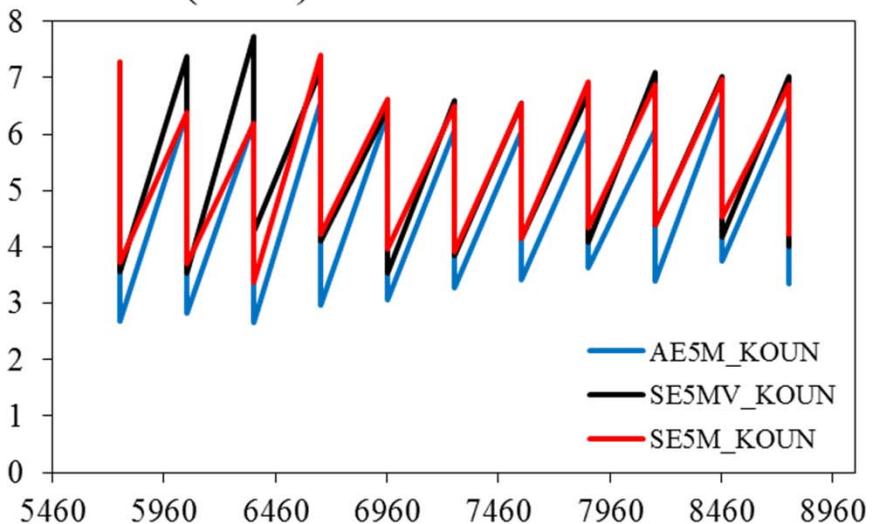
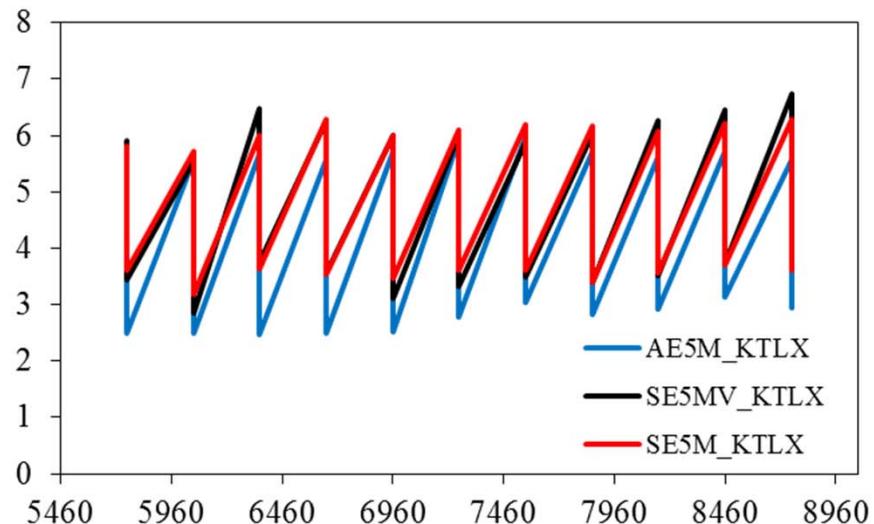
30

# Analyzed T' (shaded), Pressure (contours) and Wind Vectors at 1.5 km AGL

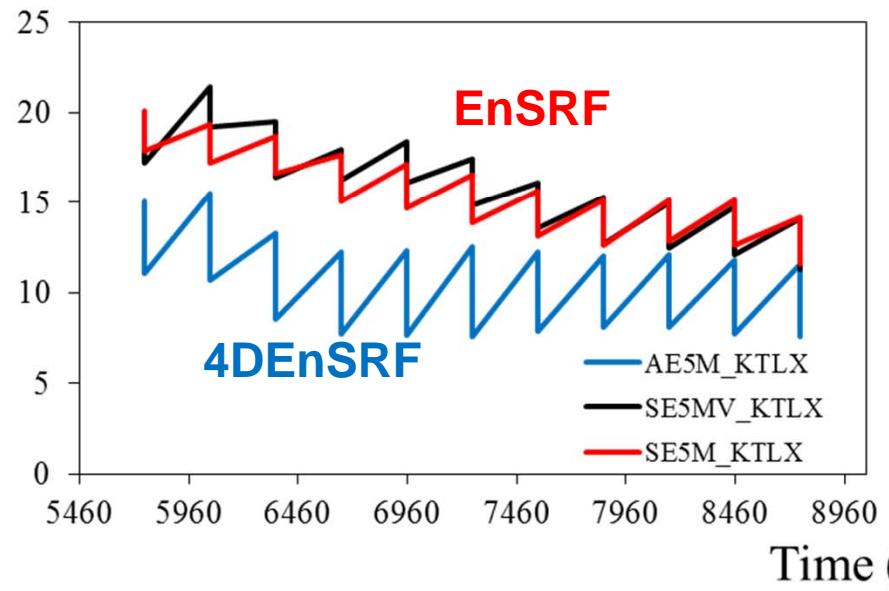


- Much better organization of low-level mesocyclone with 4DEnSRF
- Better dynamical consistency between wind, pressure and temperature fields

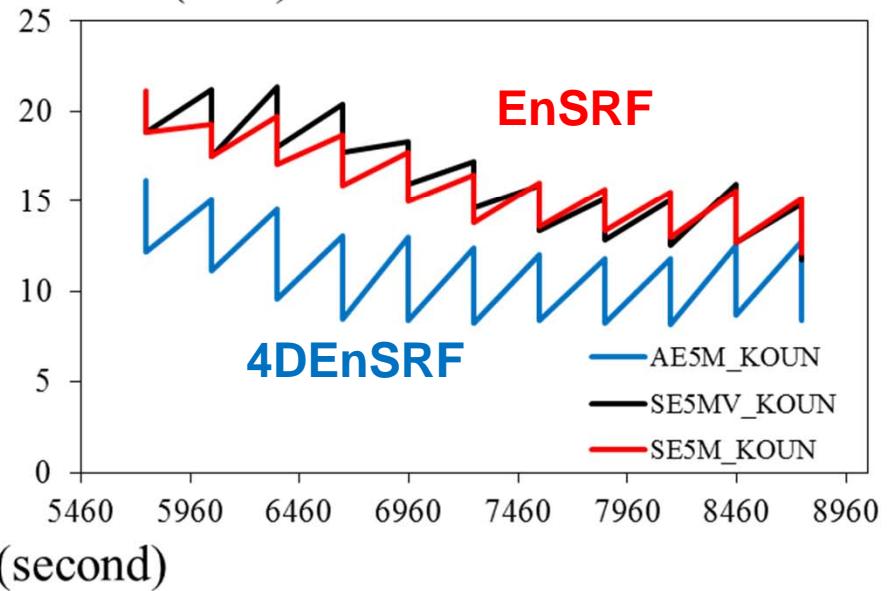
The RMS error of  $V_r$  ( $\text{m s}^{-1}$ )



The RMS error of  $Z$  (dBZ)



Against KTLX radar



Against KOUN radar

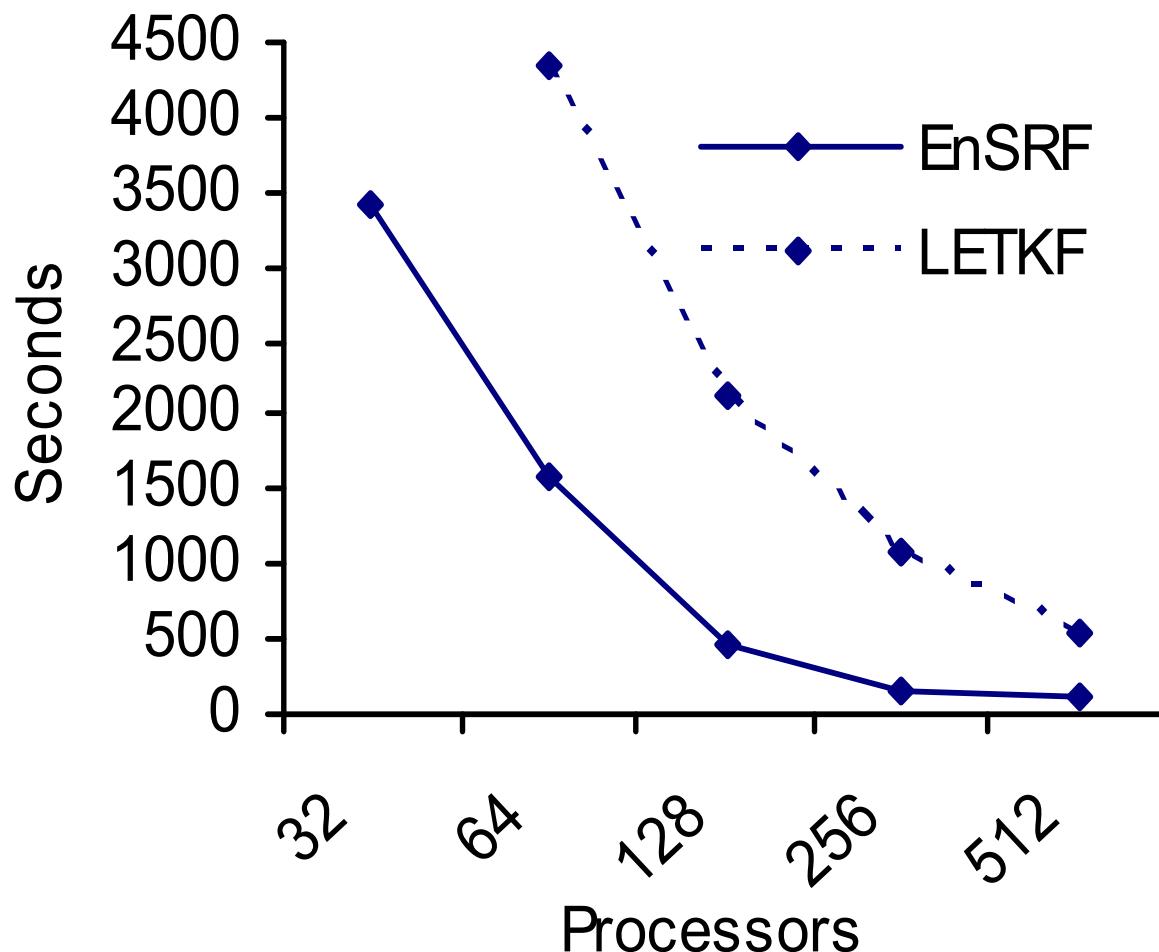
# Development of a Scalable Parallel EnSRF DA System suitable for Very-high-density Observations (e.g., WSR-88D network)

- Commonly used EnSRF is serial – observations affecting common grid points cannot be assimilated simultaneously
- Current parallel algorithms (e.g., Anderson and Collins JTec 2007, as used in DART) assimilate obs one after another, updating state variables in parallel – the algorithm is not very scalable to millions of dense obs.
- The LETKF algorithm is easier to parallelize, but the algorithm itself is more expensive.
- We employ a domain-decomposition-based hybrid OpenMP-MPI (SMP-DMP) approach for achieve better scalability for very dense observations.

(Wang, Jung, Supinie and Xue 2012) Also Poster 19.

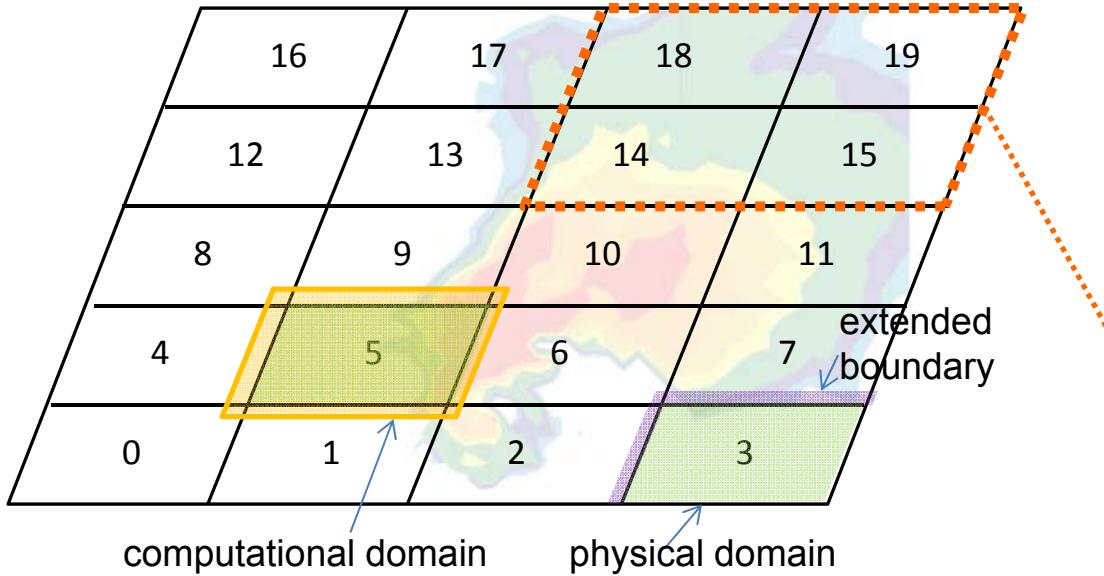
*Timing statistics of parallel EnSRF and LETKF algorithms  
for a global model test problem of moderate resolution*

(courtesy of Jeffrey Whitaker).



Here, the EnSRF parallelization is at the state vector level – observations are still assimilated one after another.

# Hybrid MPI/OpenMP Algorithm for EnSRF



- Hybrid Parallel EnKF system has been developed based on domain decomposition strategy.
- Each decomposed domain can use multiple cores on shared memory nodes via OpenMP parallelization.
- For radar data, each domain is further divided into 4 uneven-sized patches to ensure maximum parallelism.
- For conventional data, state variables within the influence radius of each observation are updated across multiple processors.

14, 15, 18, 19: physical domains

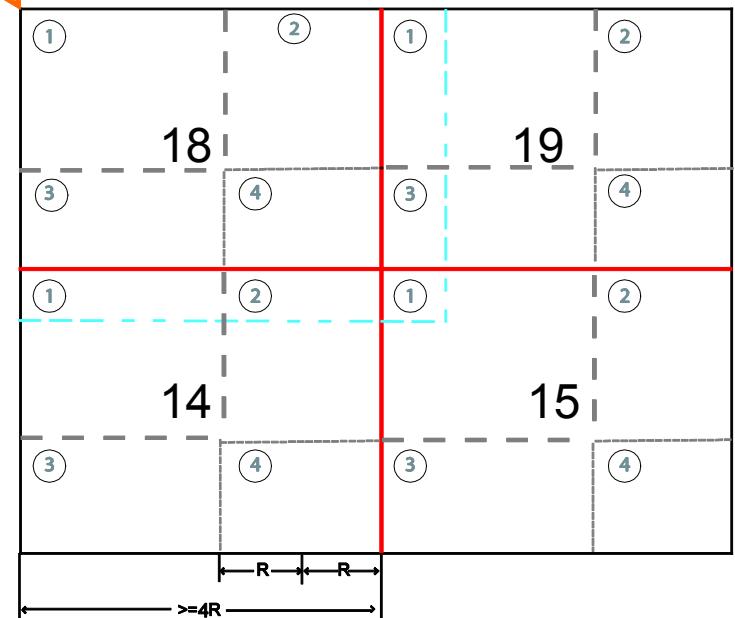
①, ②, ③, ④: sub-patches

Red: physical domain boundaries

Blue: extended boundaries

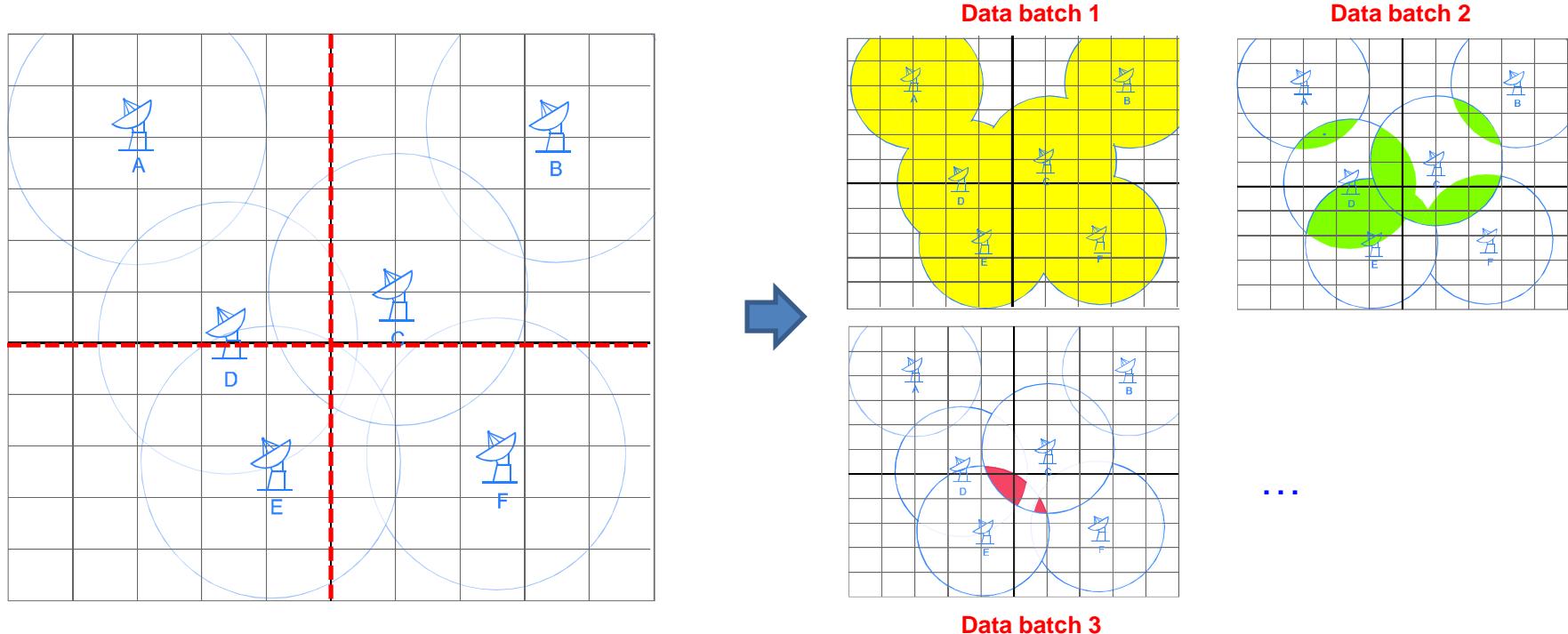
Gray: sub-patch boundaries

R: covariance localization radius



e.g.) Parallel algorithm for radar data

# Radar data reorganization

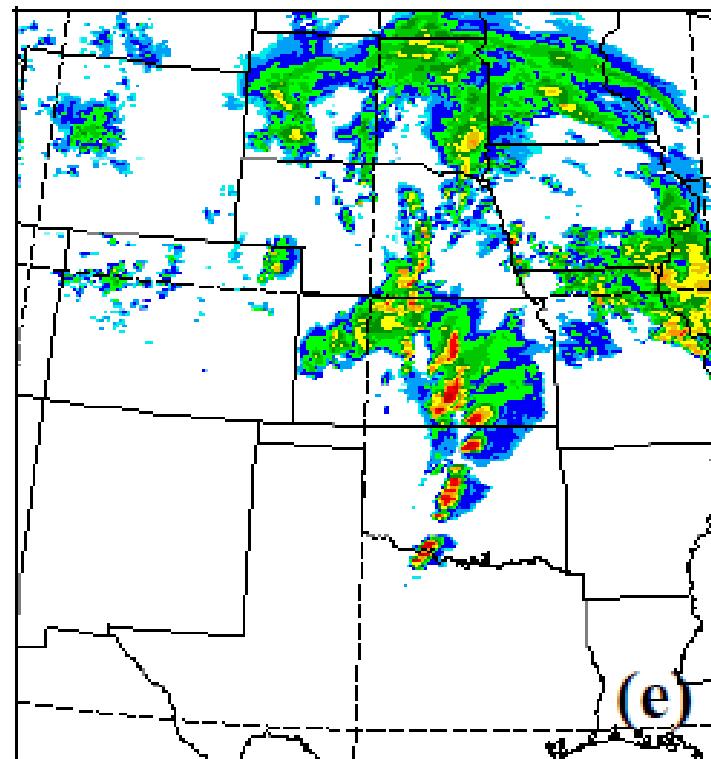


- Radar data are grouped into several batches such that no more than one column of data exists for each column of grid within each batch.
- The load imbalance issue is significantly improved for radar networks designed to maximize spatial coverage, such as the WSR-88D network.
- Suitable for very dense radar observations.

# Performance Analysis of MPI EnKF Algorithms (test with the May 10 OK-KS Tornado Outbreak)

## Model configurations

- Forecast model: ARPS
- DA scheme: parallel EnSRF
- Microphysics scheme: LFO83
- Grid configurations: **4 km grid**
- Nested inside **40 km RR ensemble**
- Physical domain: 443x483x53
- 40 ensemble members
- Observations
  - conventional data : surface, sounding, profiler (3,841 observations)
  - radar: **35 WSR-88D radars (788,145 observations)**



# Performance analysis of MPI and MPI/OpenMP hybrid EnKF algorithms

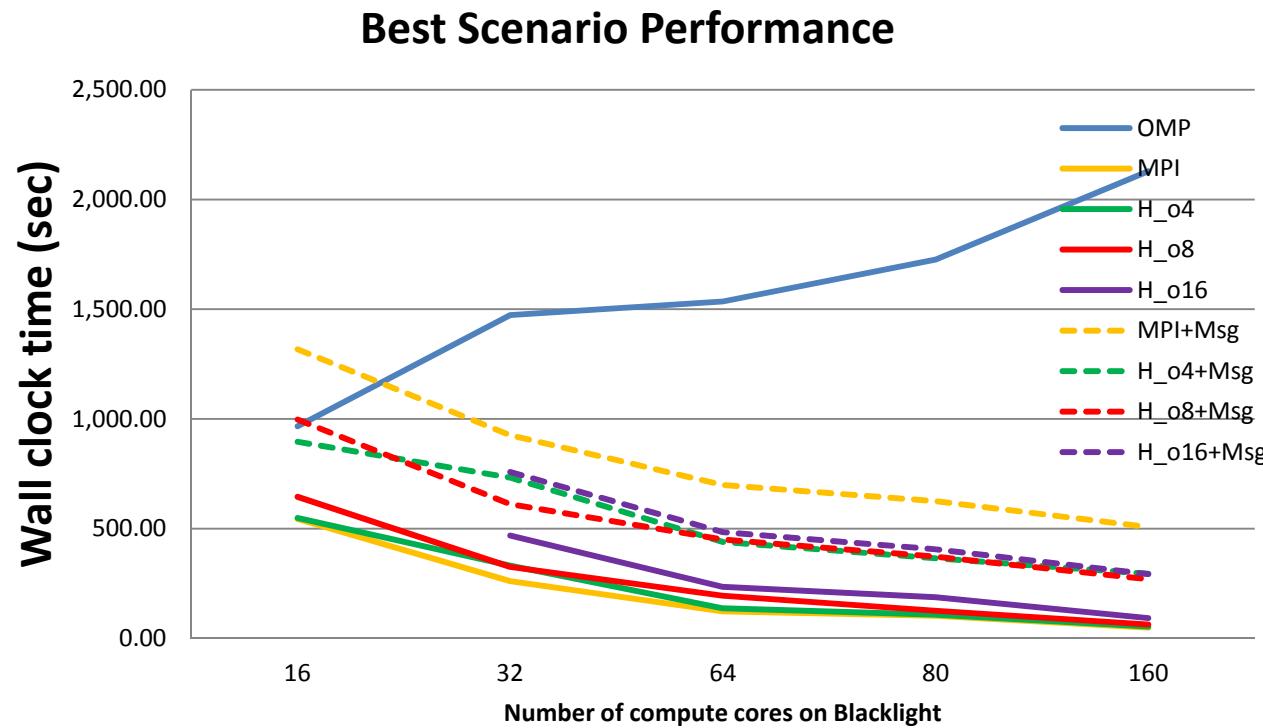
Table 3. Comparison of minimum time taken in hybrid mode with that in MPI mode using the same amount of cores on 4 compute nodes

Number of cores	Hybrid case	Minimum time	MPI case	Minimum time	Improvement
8	HYB_01x04_01_2	1,471	MPI_02x04_02_1	2169	698
16	HYB_01x04_01_4	1,129	MPI_04x04_04_1	1327	198
24	HYB_01x04_01_6	831	MPI_03x08_06_1	880	49
40	HYB_02x10_05_2	635	MPI_04x10_10_1	637	2
48	HYB_03x08_06_2	604	MPI_06x08_12_1	606	2

- Performance tests on National Institute for computational Science (NICS) supercomputer.
- The hybrid mode is usually faster than MPI mode with optimal setting.
- The hybrid and MPI wall clock time is sensitive to the domain partitioning and # of core/node configurations.
- Case-dependent and system-dependent.
- The hybrid distributed-shared-memory parallel mode helps reduce explicit data communication within a node and improve load balance across nodes.

# Performance analysis of MPI EnKF algorithms

- PSC Blacklight
  - SGI UV 1000 cc-NUMA shared-memory system
  - 2 Intel Xeon X7569 eight-core processors per node
  - Radar assimilation: **48 sec excluding I/O and message passing (10 x 16 subdomains)**



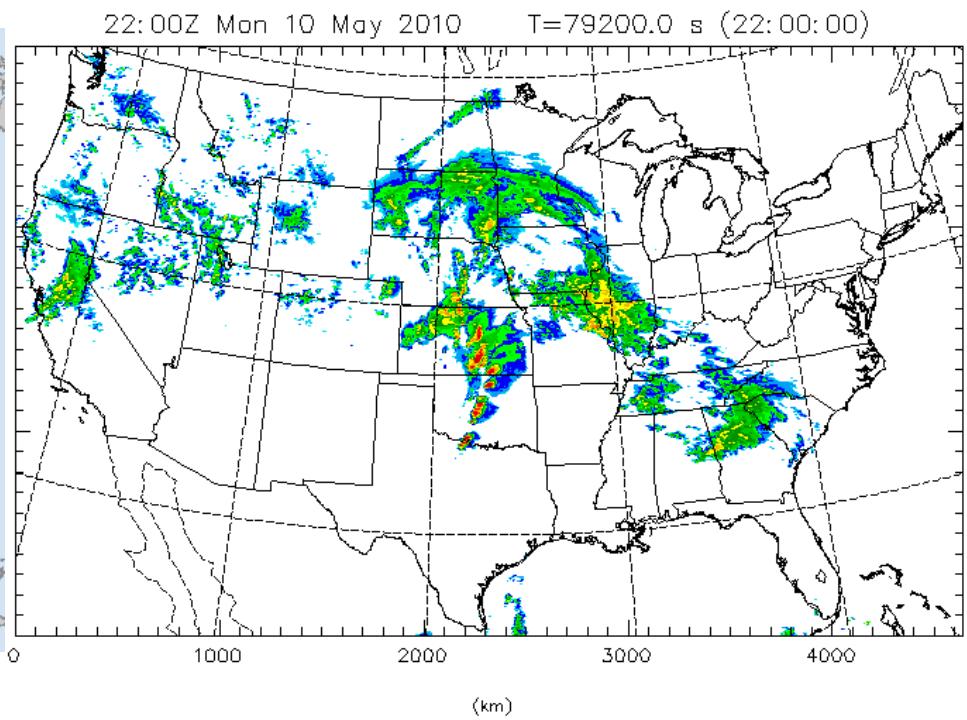
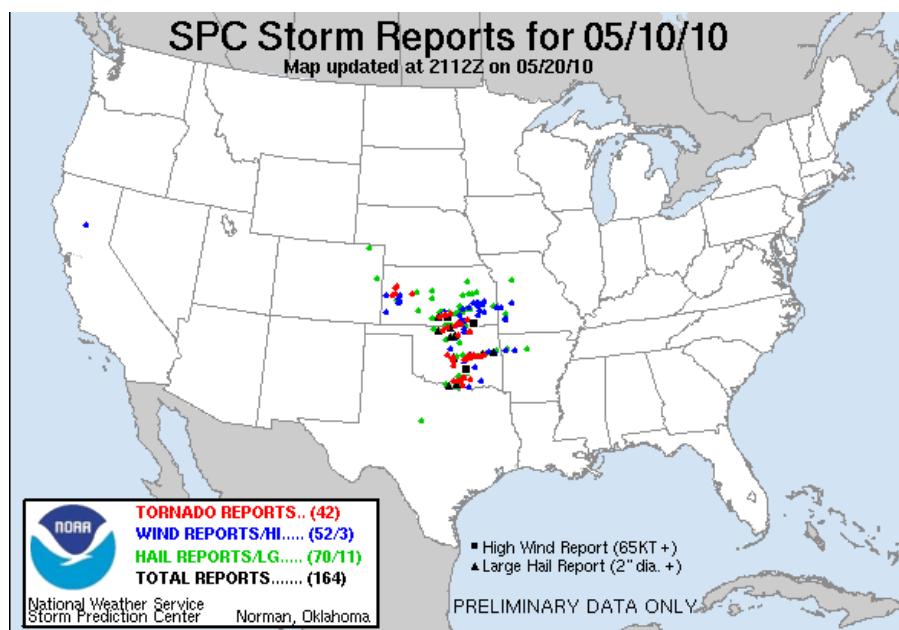
“H” stands for hybrid, “\_ox” for the number of OMP threads, dashed: I/O and message.

# Performance analysis of MPI EnKF algorithms

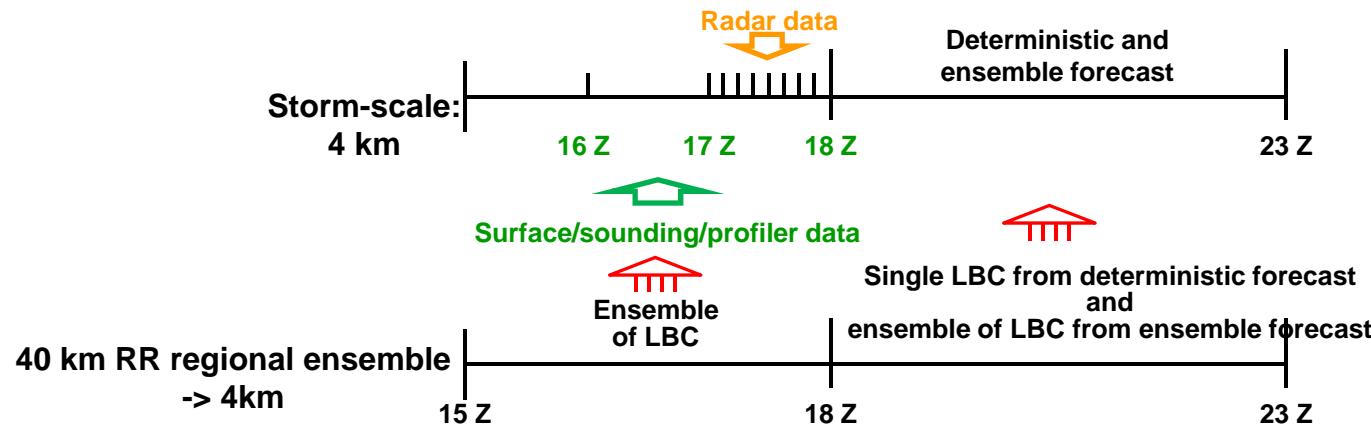
- Kraken (4 x 6 PEs x 3 threads)
  - Two 2.6 GHZ six-core-AMD Opteron processors
  - Peak performance: 1.17 Pflops
  - Radar assimilation: 1.99 min excluding only IO (4x6 subdomains)
- Sooner (4 x 8 PEs x 8 threads)
  - Pentium5 Xeon EM64T quad core “Harpertown” E5405 2.0 GHz
  - Peak performance: 34 Tflops
  - Radar assimilation: 4.18 min
  - Conventional (surface, sounding, profiler) data assimilation: 2.11 min
  - Radar + conventional data: 6.96 min (4x8 subdomains)

# 10 May 2010 Oklahoma-Kansas tornado outbreak

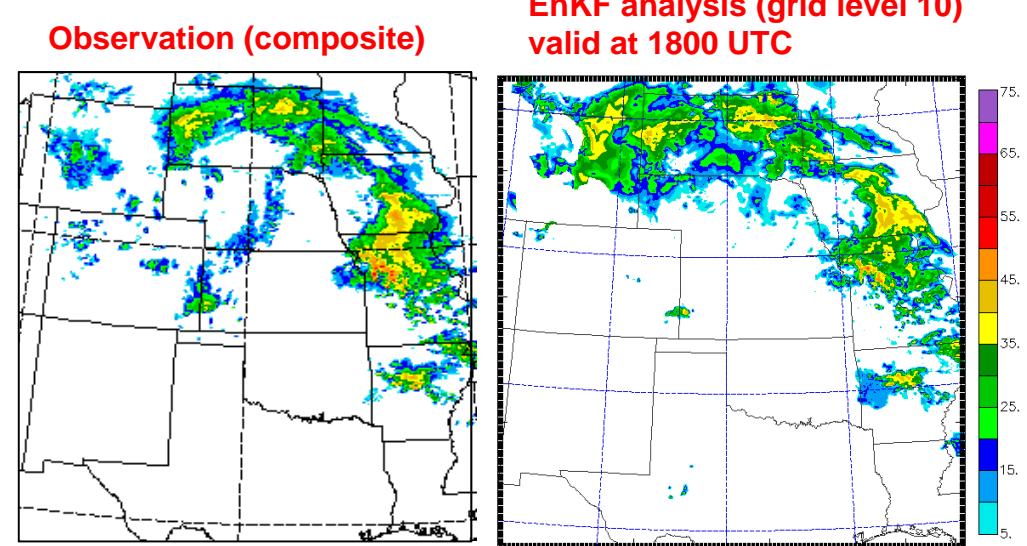
- Over 40 tornadoes, with up to EF4 intensity in OK and KS



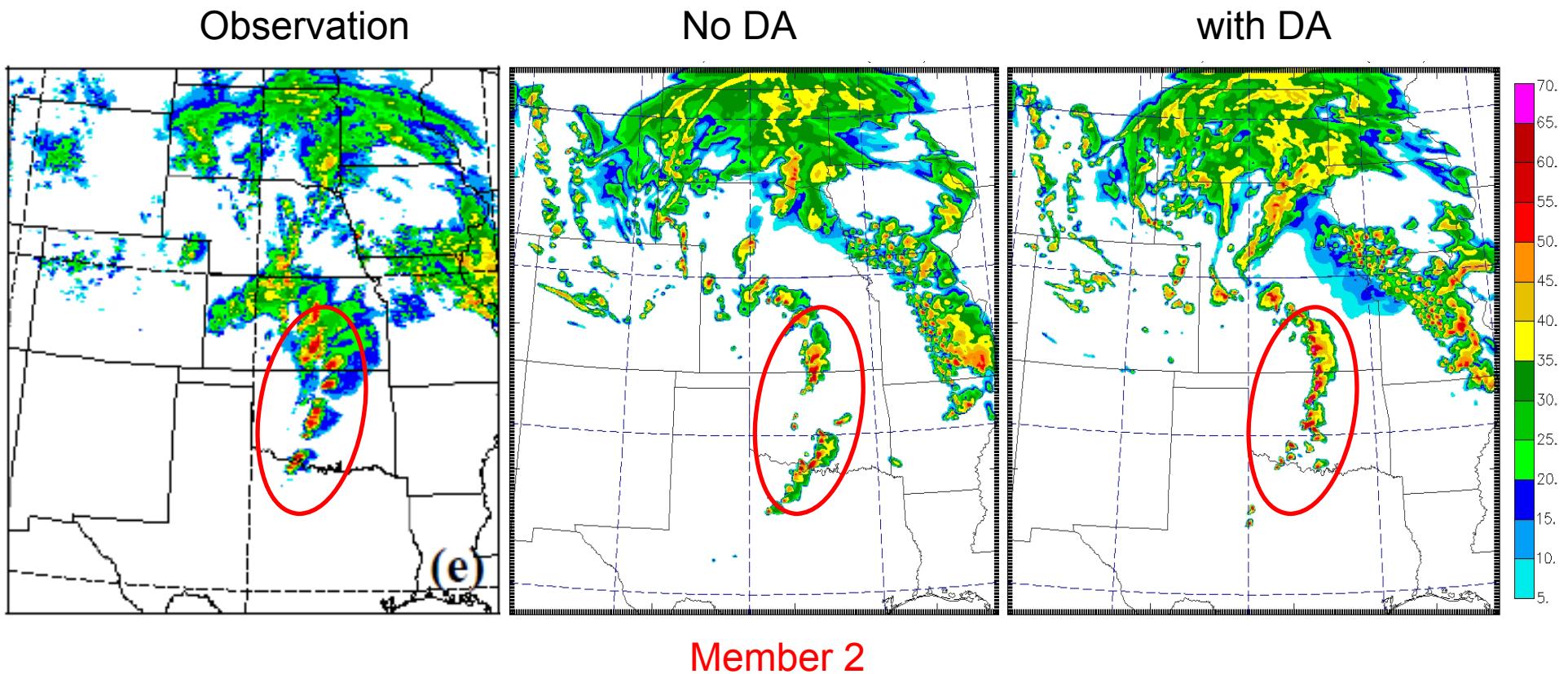
# Experiments



- noDA: no additional data
  - Start from 40 km RR regional ensemble interpolated to 4 km at 1500 UTC
- CNTL
  - Conventional data: 1600, 1700, 1800 UTC
  - Radar data: 1705 – 1800 UTC (5 min. interval)

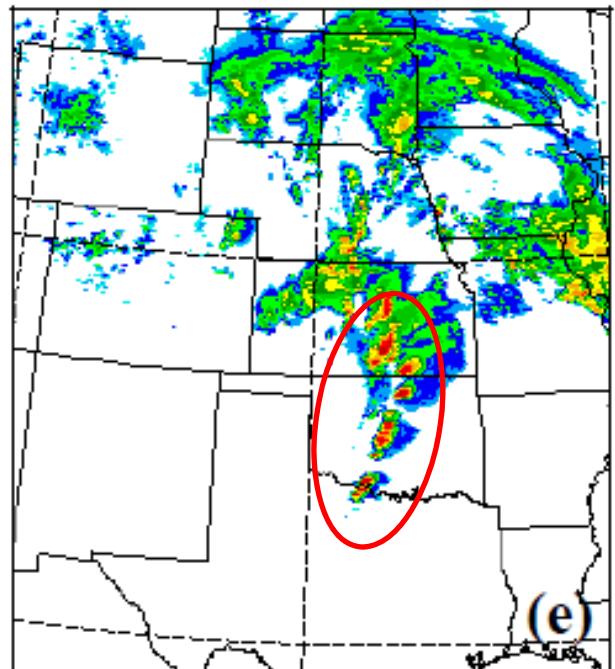


# Ensemble forecasts valid at 2200 UTC

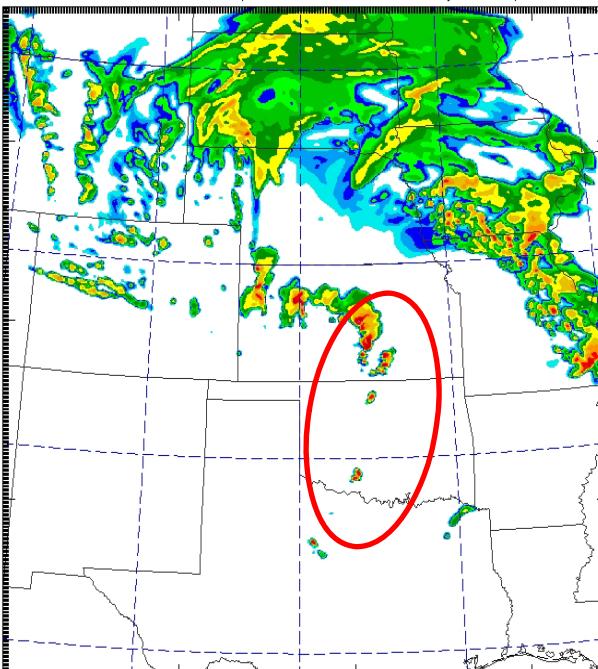


# Ensemble forecasts valid at 2200 UTC

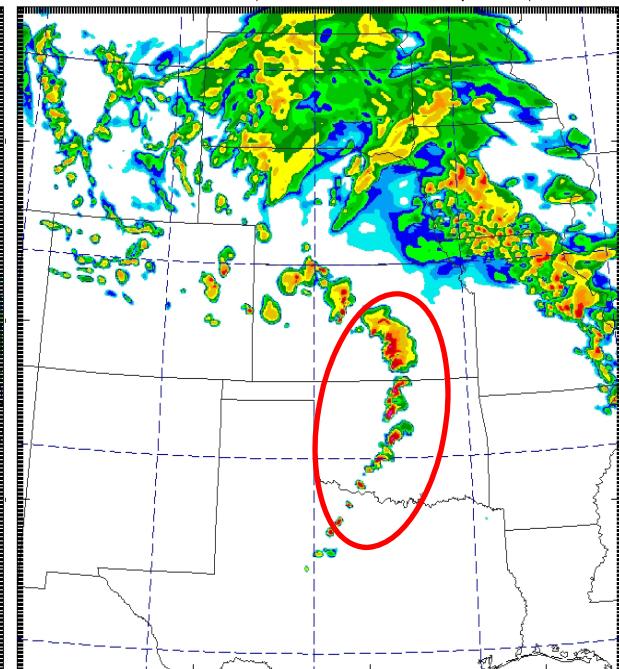
Observation



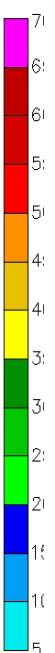
No DA



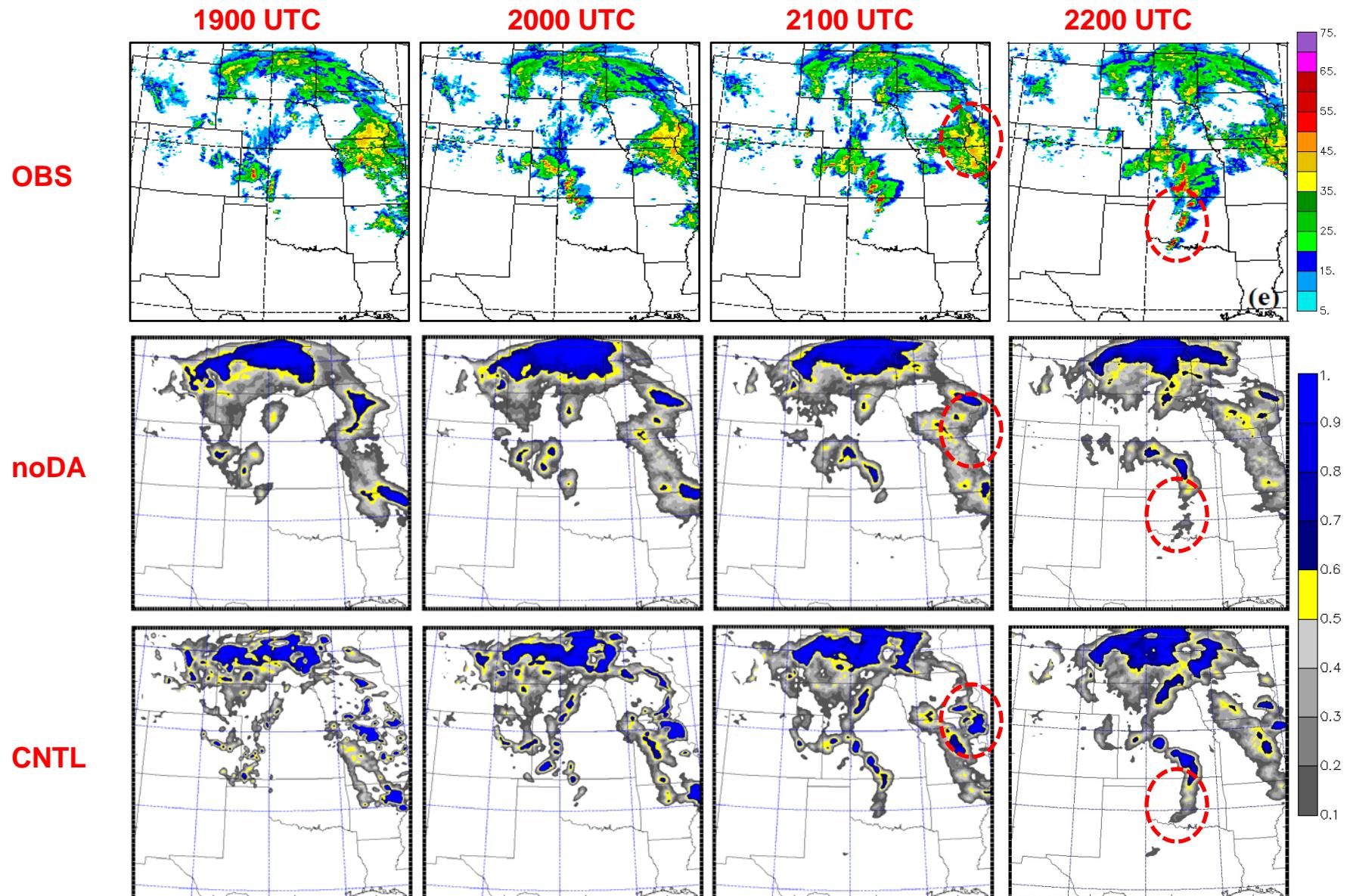
with DA



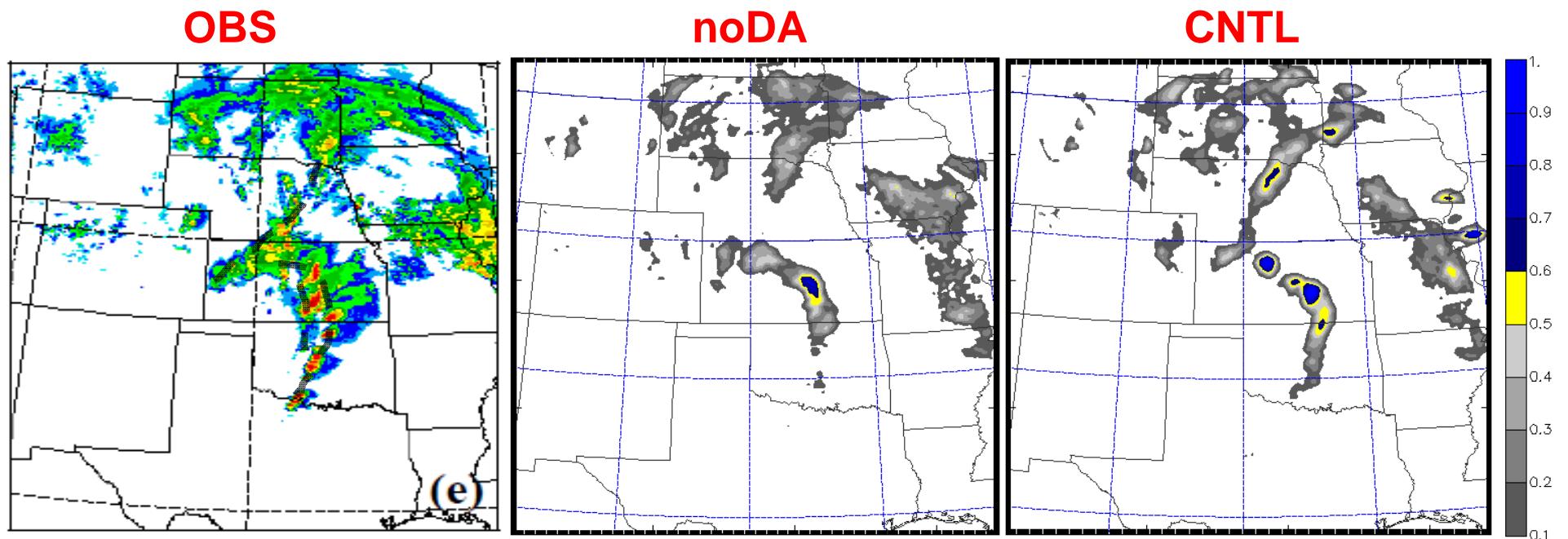
Member 12



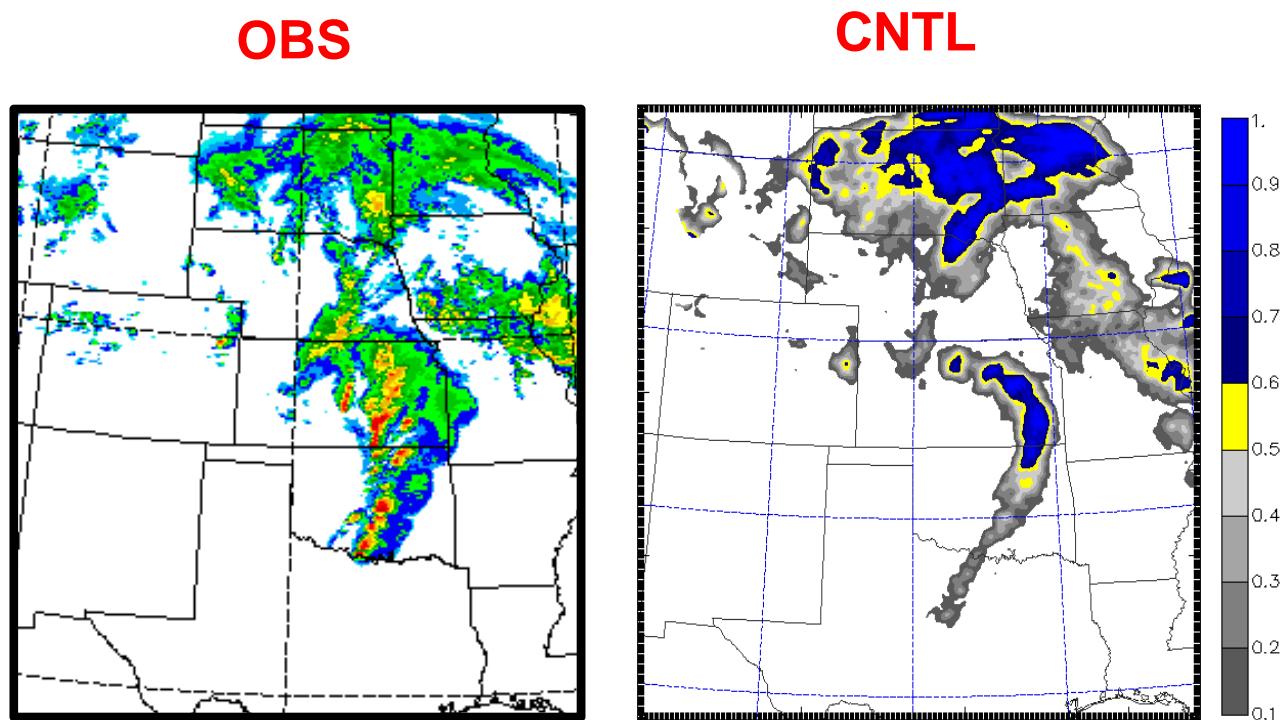
# Ensemble forecast probability for $Z_H > 25$ dBZ at $z = 2\text{km}$



Ensemble forecast probability for  $Z_H > 35$  dBZ valid  
at 2200 UTC (t=4 h) at z = 2km



Ensemble forecasts probability for  $Z_H > 25$  dBZ  
valid at 2300 UTC (t=5 h) at z = 2km



# LETKF for Doppler Radar Data

Local Ensemble Transform Kalman Filter (LETKF)

- Update for each state variable can be done in **parallel** (Hunt et al 2007).
- **Scales** to high-dimensional systems and large numbers of observations.
- LETKF has **not been applied** to applied to storm-scale radar DA before

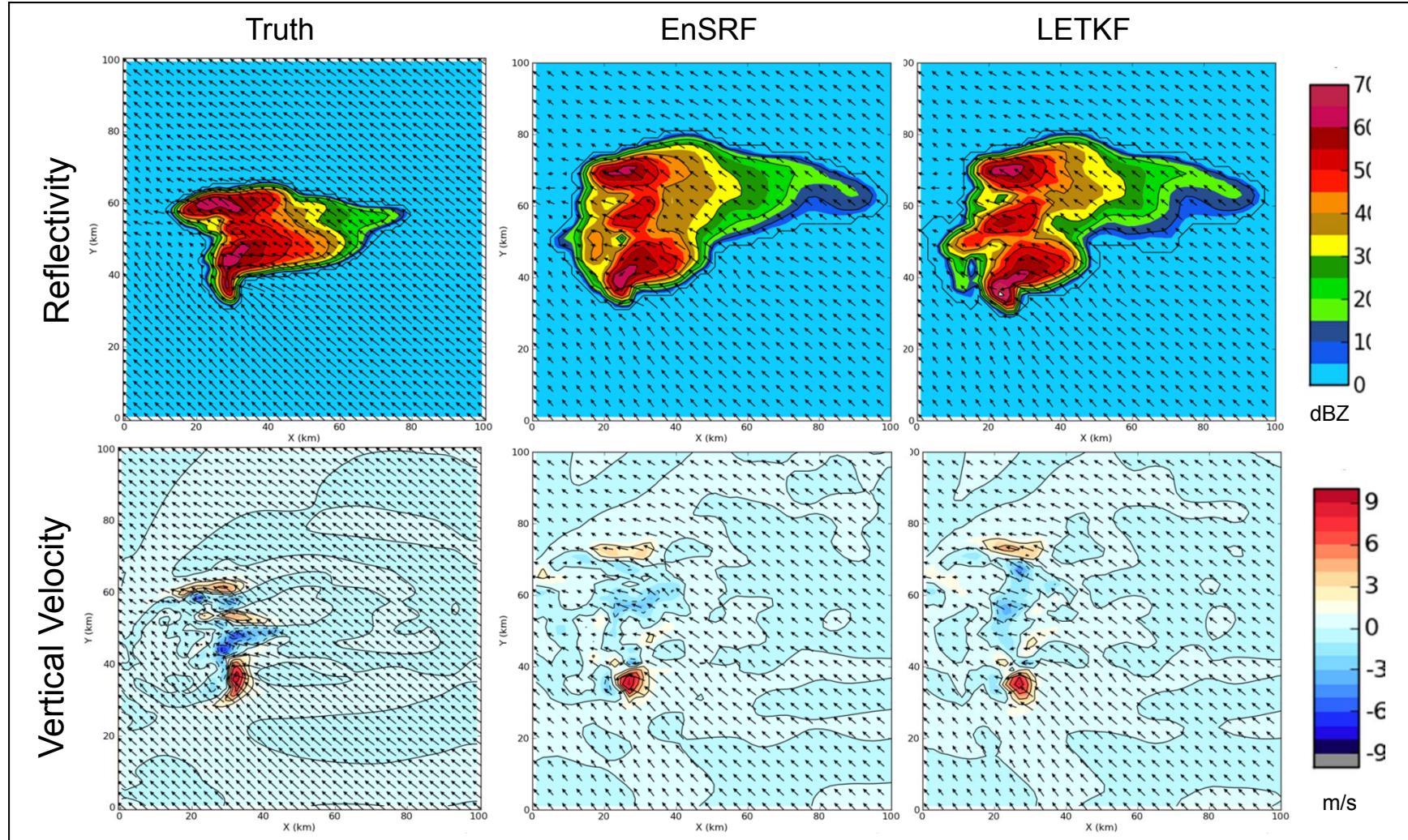
**Poster 14:** Doppler Radar Data Assimilation Using a LETKF (Terra Thompson)

**Poster 22:** Implementation of LETKF with ARPS model and some preliminary results of OSSE (Gang Zhao)

# LETKF Implementation (NSSL Version)

- Built upon the LETKF kernel/core Fortran code by Takemasa Miyoshi (2010).
  - LETKF is developed for the cloud model, NCOMMAS.
  - System is a Python-Fortran hybrid.
- 
- **OSSE experiments**: supercell environment, 2 km horizontal grid, 15 ensemble members, assimilation of radial velocity observations every 2 minutes for 40 minutes.

# Preliminary Results (work in progress)



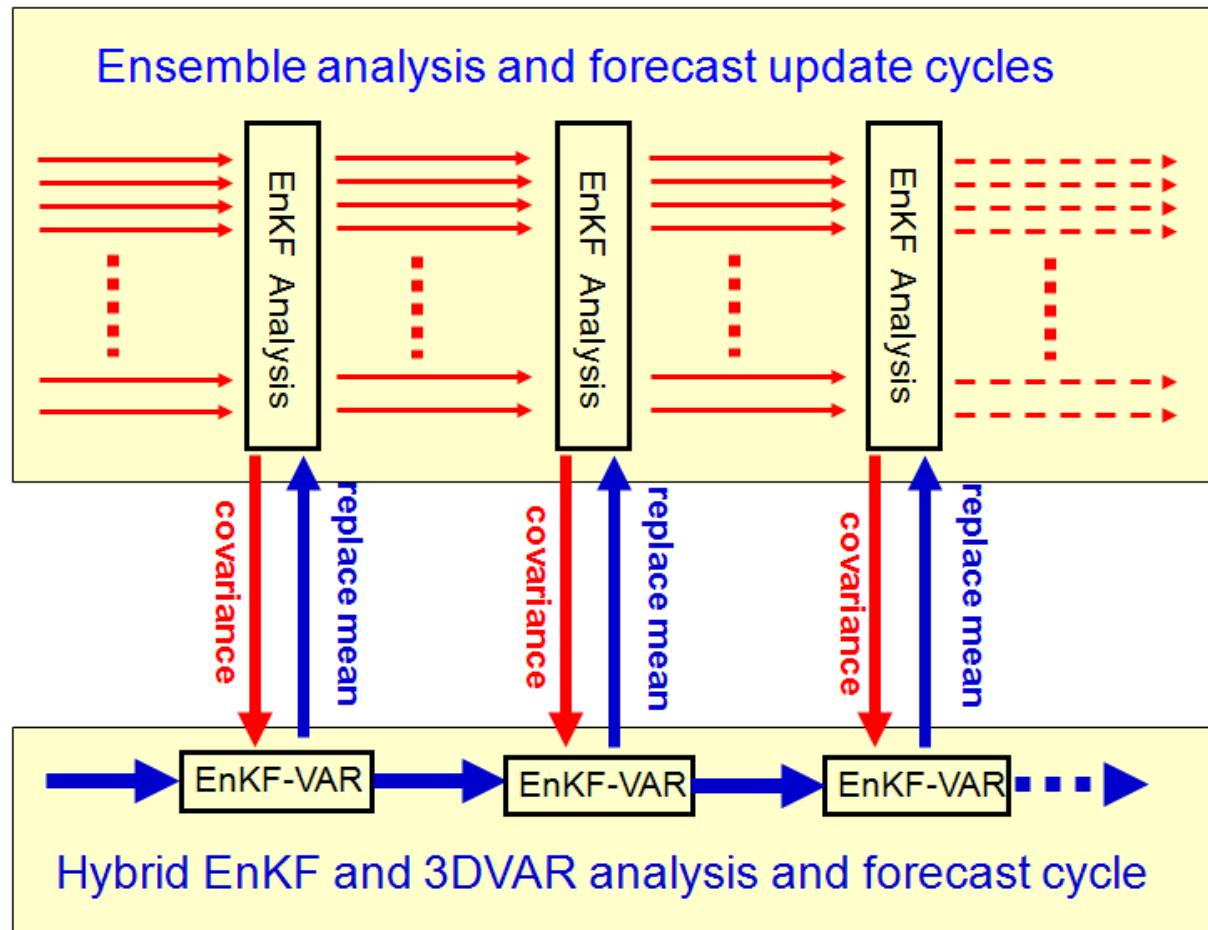
For more details see “Doppler Radar Data Assimilation Using a LETKF” poster by Terra Thompson, Lou Wicker, Xuguang Wang.

Analyses after 40 min of 2 min cycles, only Vr data were used

# Hybrid Variational-Ensemble DA

- Combines the strengths of variational (VAR) and ensemble DA methods
- Allows VAR to use flow-dependent background error covariance  $P$ .
- Allows the inclusion/use of equation constraints (including full model equations in 4DVAR)
- Allows model-space localization for correctly handling non-local observations (e.g., radiance, attenuated reflectivity)
- For small ensembles, combination of static  $B$  and  $P$  promises to give better results than  $P$  alone.
- Ease the transition from currently operational 3DVAR to eventual ensemble-4DVAR hybrid.
- Direction that NCEP, UK Met Office, Env. Canada, etc. are taking.

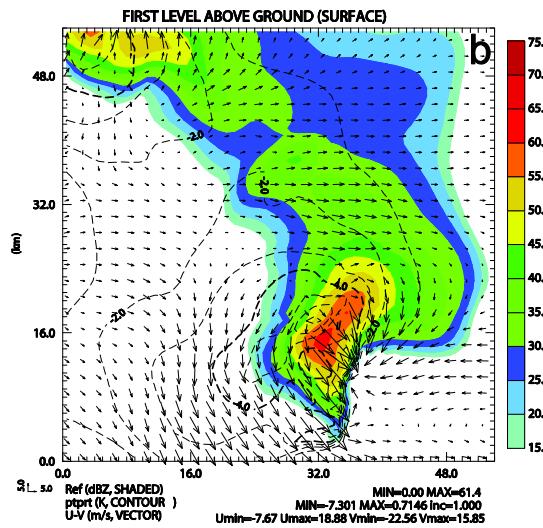
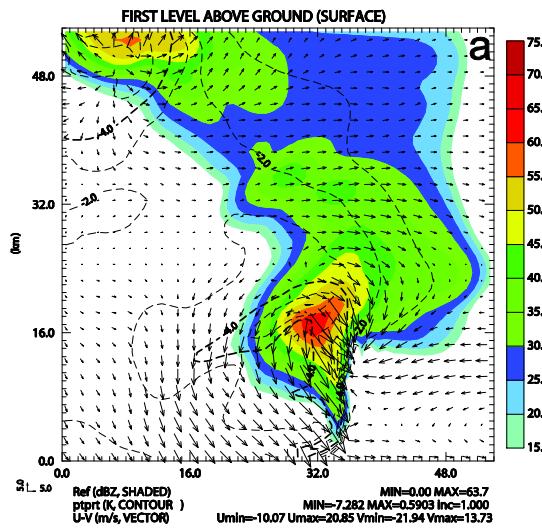
# ARPS Hybrid 3DVAR-EnKF Data Assimilation System



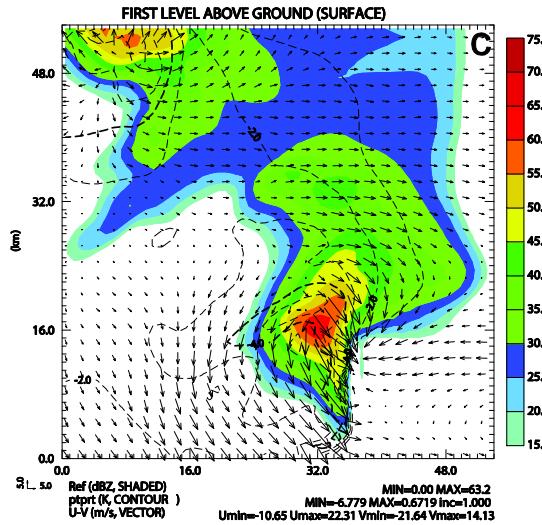
Gao, Xue and Stensrud (2010 SLS)

**$\theta'$ (contours), Z(color shades) and  $V_h$  (vectors) at Surface  
at the End of the 80 Min. DA Cycles with single radar**

Truth

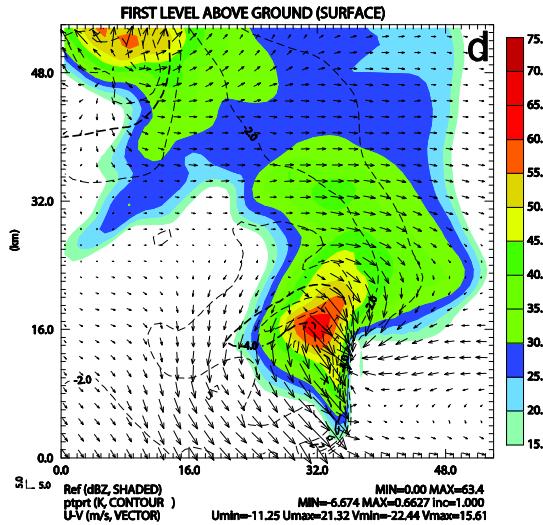


Pure EnKF

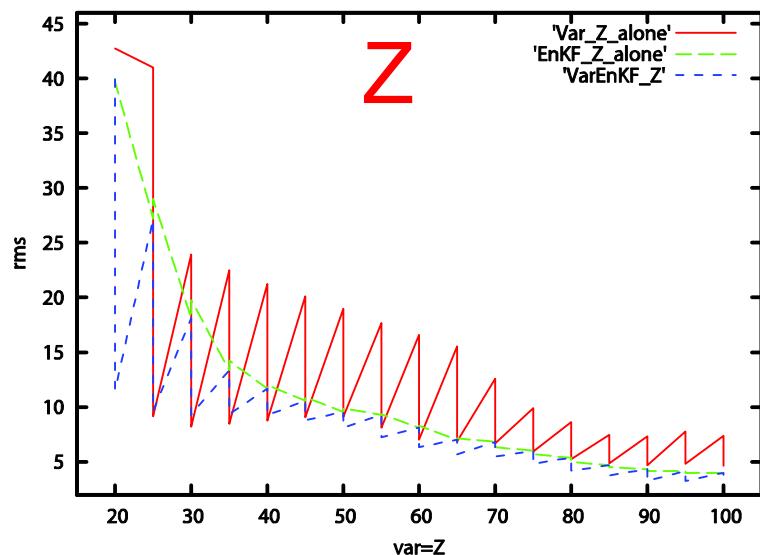
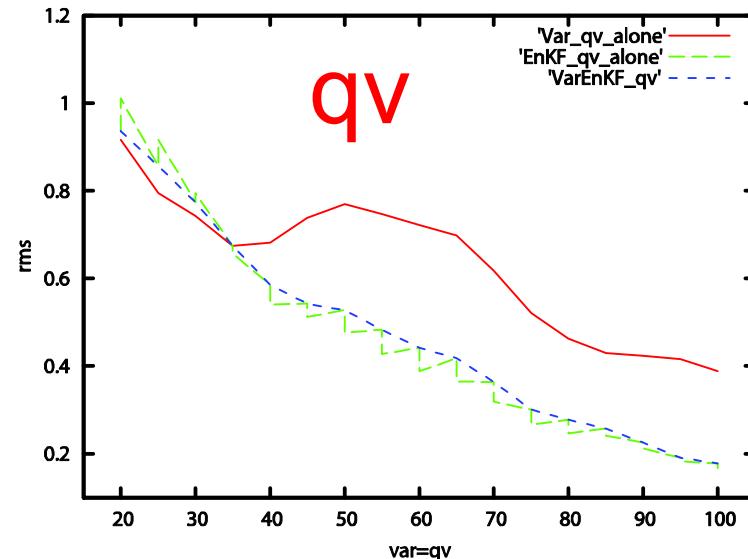
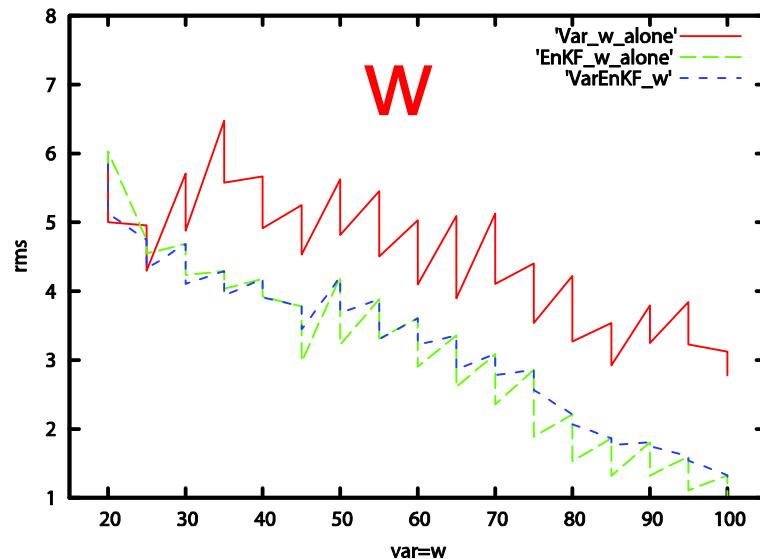


3DVAR

Hybrid



# Analysis RMS Errors with Radar from One Radar



Red: 3DVAR

Green: Pure EnKF

Blue: 3DVAR-EnKF hybrid,  
100% flow-dependent P

# Assimilating Reflectivity Within a 3DVAR Framework

Previous research:

- > 4DVAR technique (Sun and Crook 1997;1998);
- > EnKF (Tong and Xue 2005; Dowell, Wicker and Synder, 2011);
- > Cloud Analysis method (Alber et al. 1996; Brewster et al. 2005; Hu et al. 2006; Weygandt and Benjamin et al. 2008);
- > MM5 3DVAR (Xiao et al. 2005), 3.5VAR (Zhao et al. 2008)

This study is trying to assimilate reflectivity in a unified 3DVAR framework by including ice hydrometeors and partition of hydrometeors using temperature field from NWP model.  
(Gao and Stensrud, 2011, *J. Atmos. Sci.* Accepted).

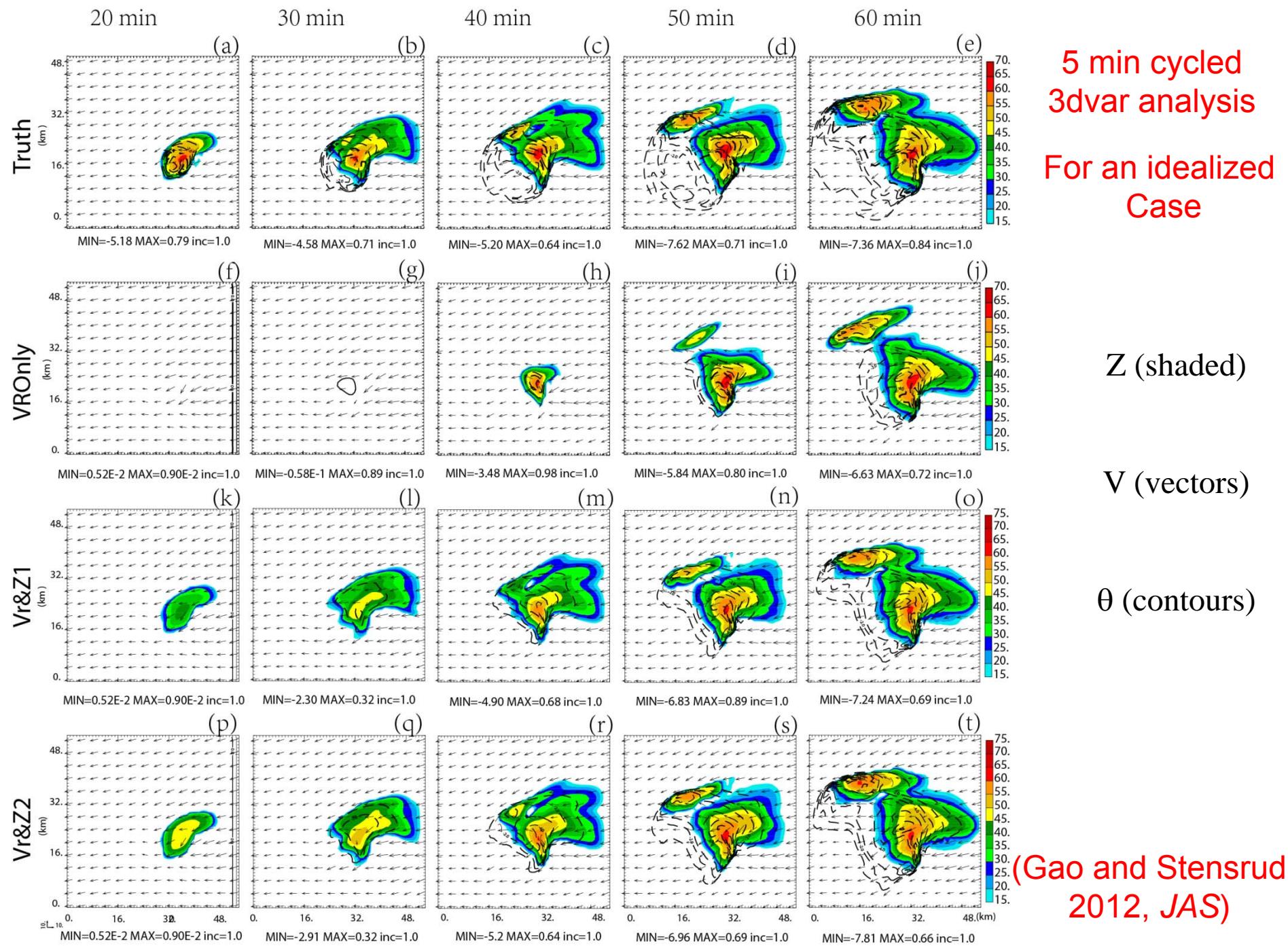
# Assimilating Reflectivity Within a 3DVAR Framework

- First method (1)
  - total reflectivity computed as:

$$Z_e = Z_{er}(q_r) + Z_{es}(q_s) + Z_{eh}(q_h), \quad (1)$$

- Second method (2)
  - partition reflectivity via temperature from NWP model output.
    - $T > +5^\circ C$ : all rain
    - $T < -5^\circ C$ : all snow and hail
    - $-5^\circ C > T > -5^\circ C$ : mixed phase
  - linearly partition reflectivity between rain and ice

$$Z_e = \begin{cases} Z_{er}(q_r) & T_b > 5^\circ C \\ Z_{es}(q_s) + Z_{eh}(q_h) & T_b > -5^\circ C \\ \alpha Z_{er}(q_r) + (1-\alpha)[Z_{es}(q_s) + Z_{eh}(q_h)] & -5^\circ C < T_b < 5^\circ C \end{cases} \quad (2)$$



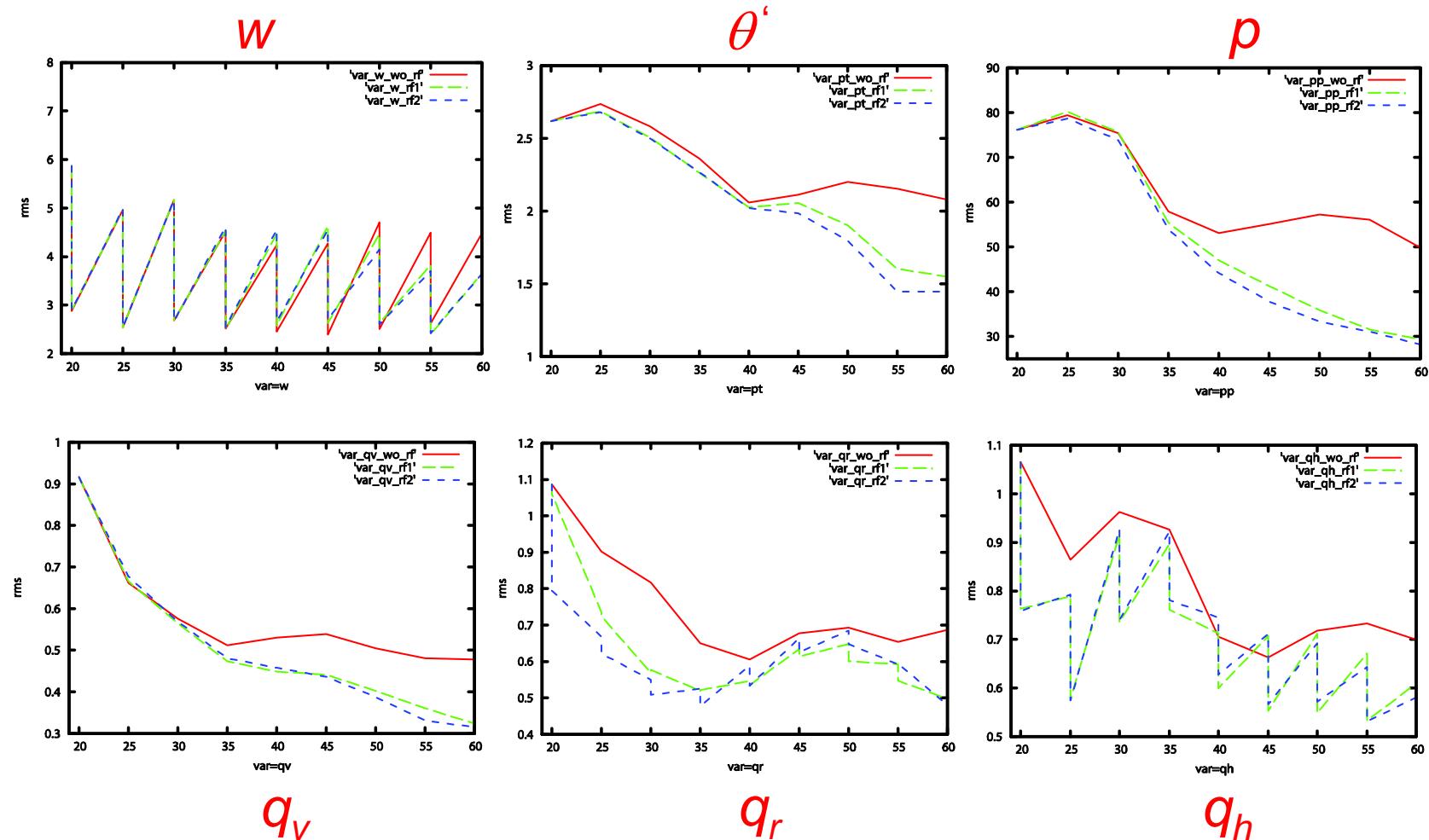
θ (contours)

V (vectors)

Z (shaded)

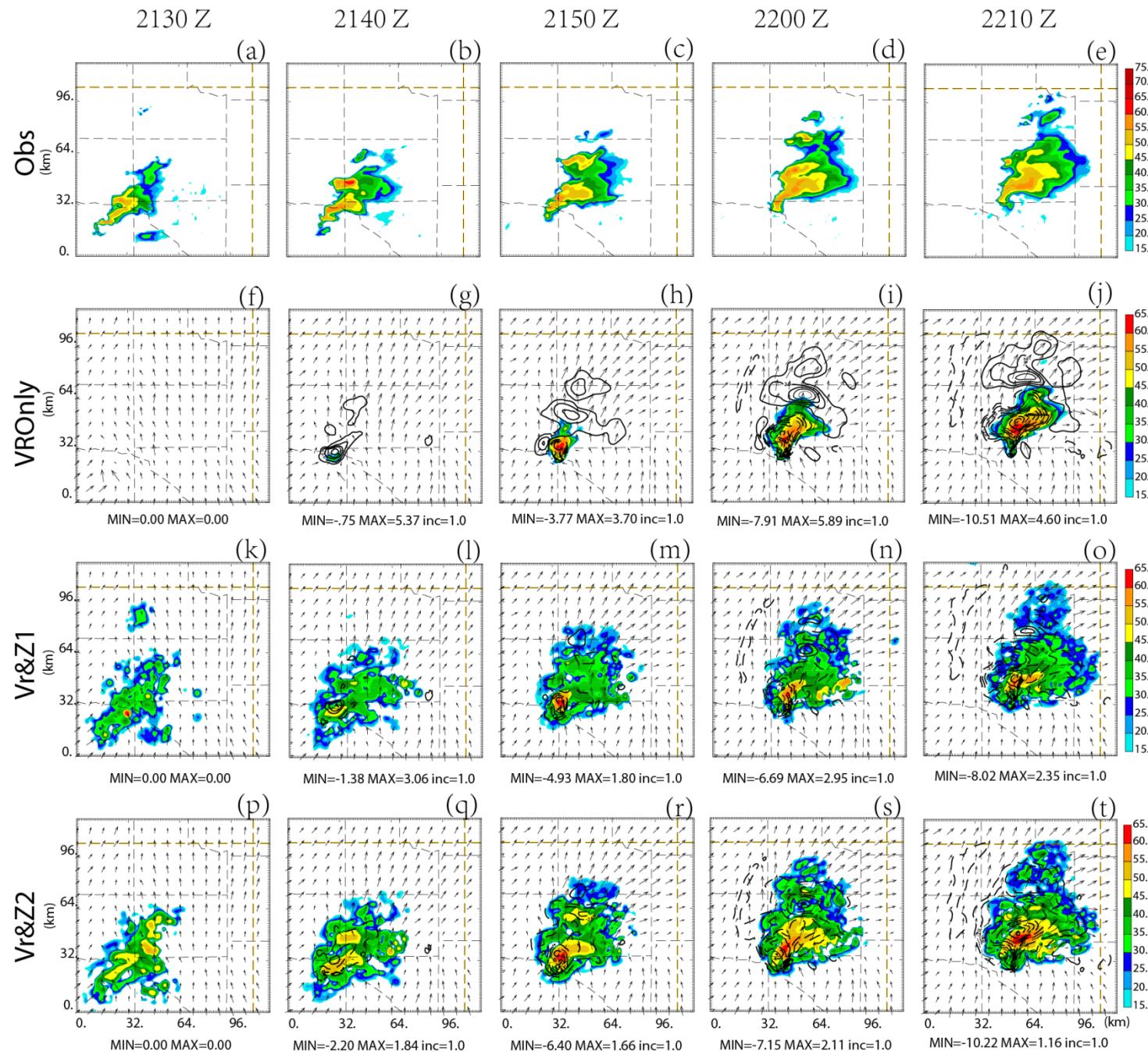
(Gao and Stensrud,  
2012, JAS)

## RMS Errors of the Analyses for 6 model variables



Red real line is for Vr only; dashed green is for Vr&Z(1) and the dashed blue is for Vr&Z(2)

## May 8, 2003 OKC Tornadic Supercell case



Z (shaded)

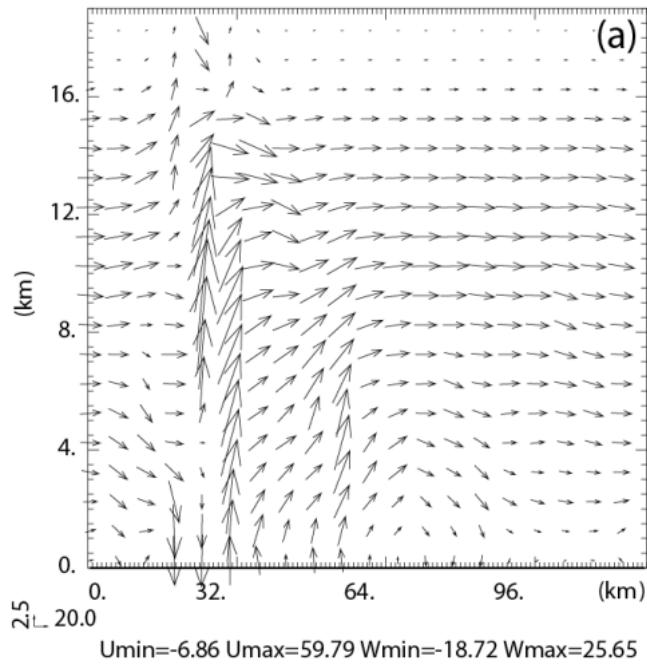
V (vectors)

$\theta$  (contours)

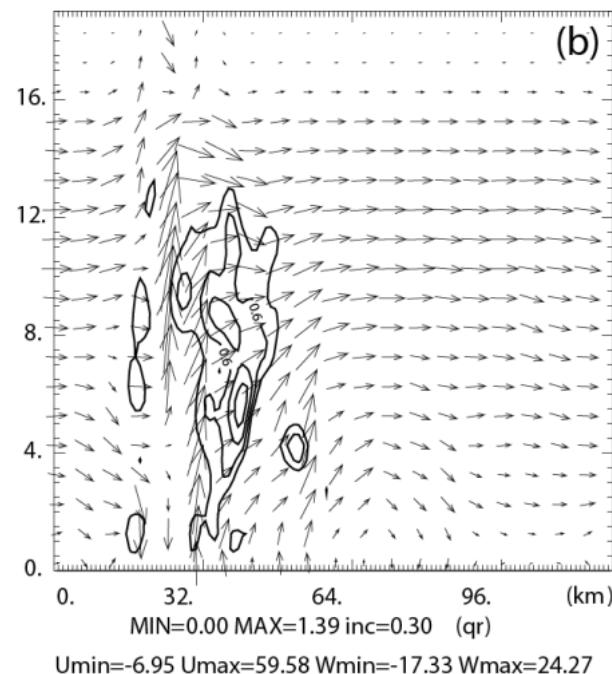
Poster 6

(Gao and Stensrud,  
2012, JAS)

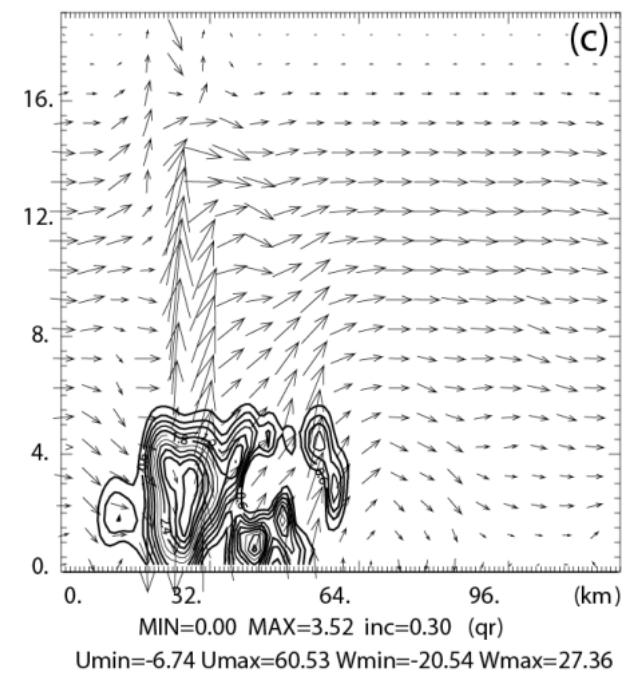
Vr Only



Vr & Z (1)



Vr & Z (2)

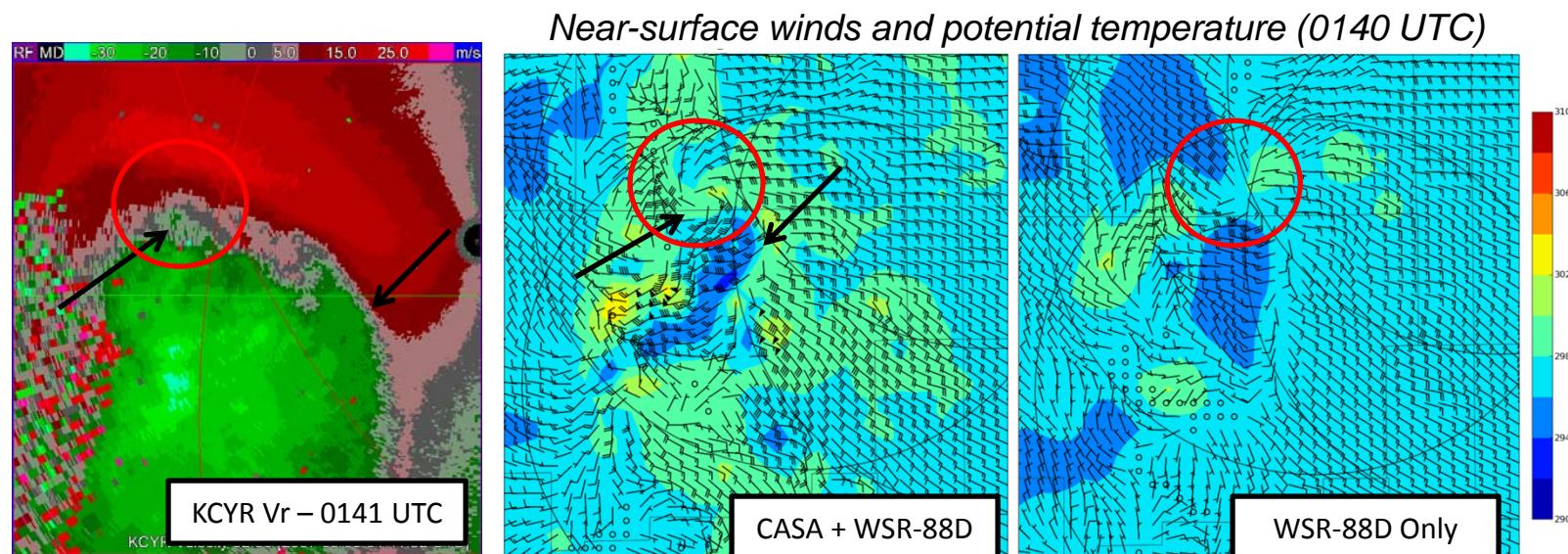
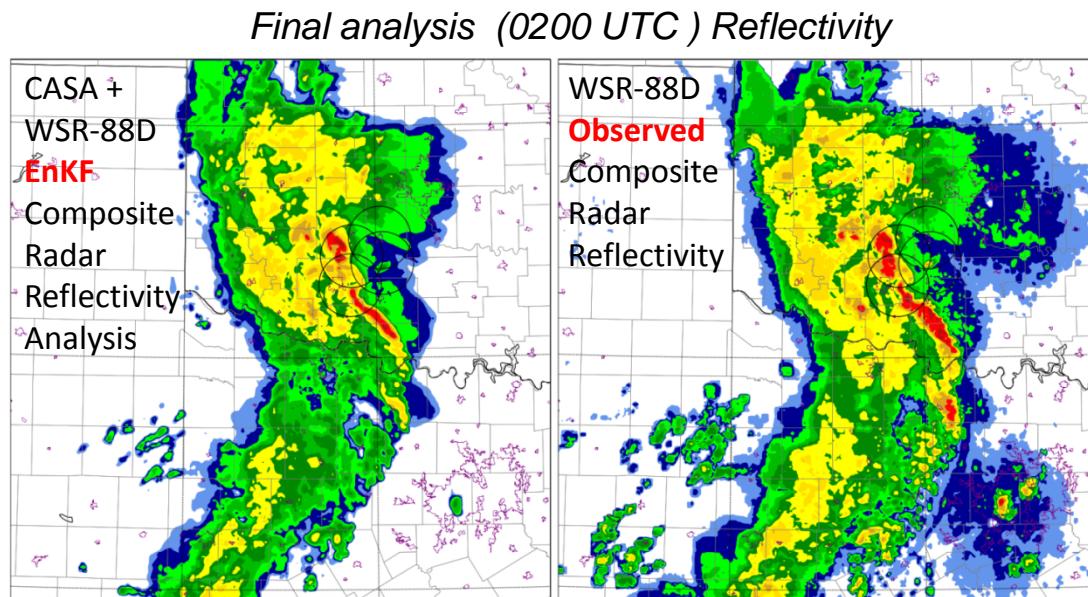


A x-z vertical slice for  $V$  ( $\text{m s}^{-1}$ ), qr (contours)

At 2130 UTC, 8 May 2003 OKC supercell storm

# Assimilation of CASA and 88D radar data using mixed-microphysics ensemble: Results of EnKF Analysis using $dx=2\text{km}$

Nathan Snook  
Talk Thursday



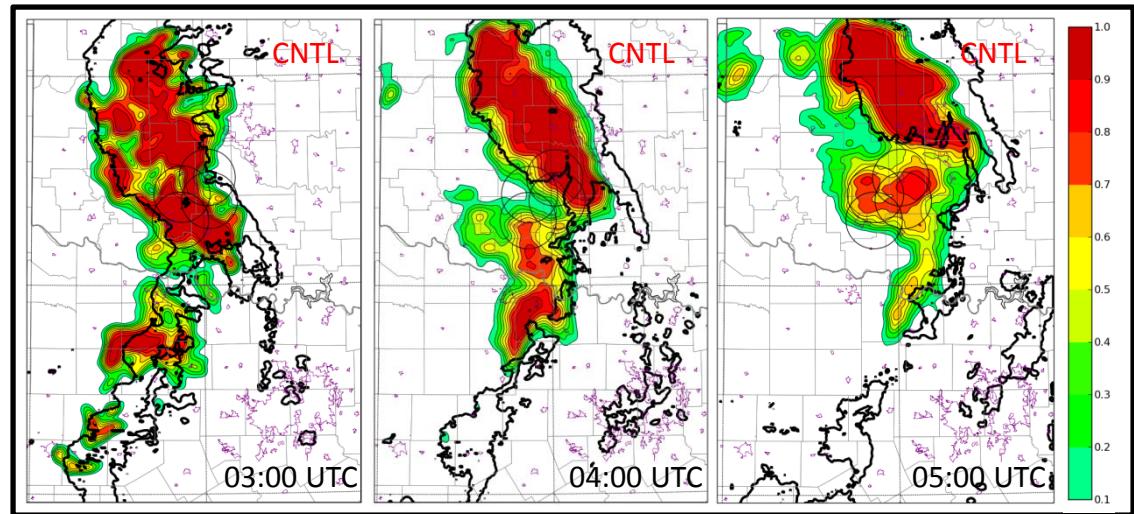
Snook et al  
(MWR 2011)

See also  
Snook's Talk

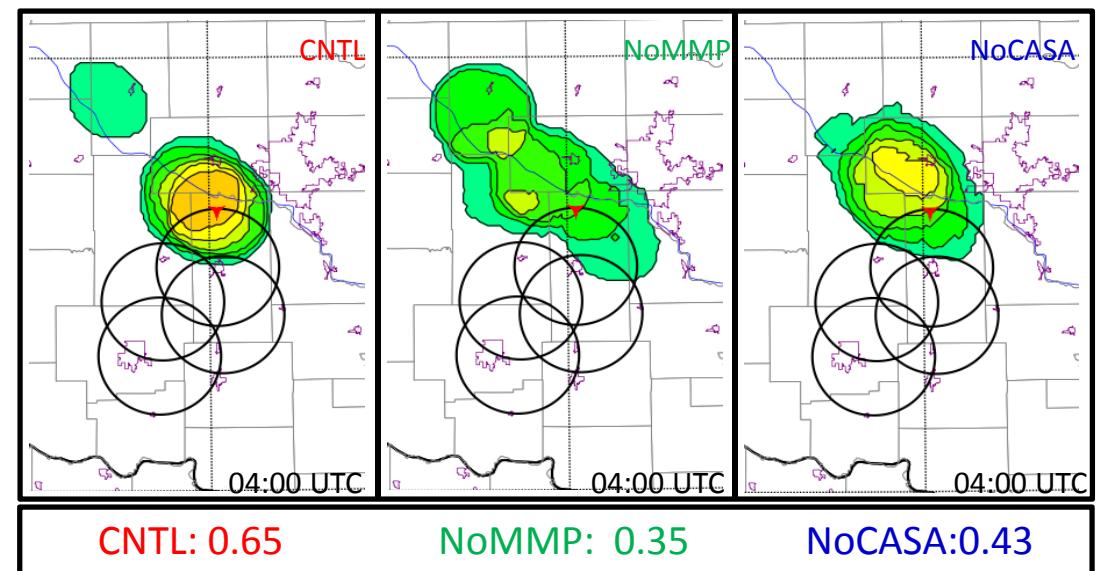
# Effects of assimilated CASA data and mixed-microphysics ensemble Ensemble-based Probabilistic Convective-scale Forecasts

- Probabilistic ensemble forecasts were generated from the final analysis state at 0200 UTC.
- For probabilistic prediction of radar reflectivity, areas of highest probability match well in placement and motion compared with observed 25 dBZ threshold.
- Assimilation of CASA radar data and use of a mixed-microphysics ensemble improved probabilistic vortex prediction; promising results were obtained predicting tornadic meso-vortices on timescales of 0-3 hours.

1, 2, and 3-Hour Probabilistic Forecasts for  $P[Z > 25 \text{ dBZ}]$

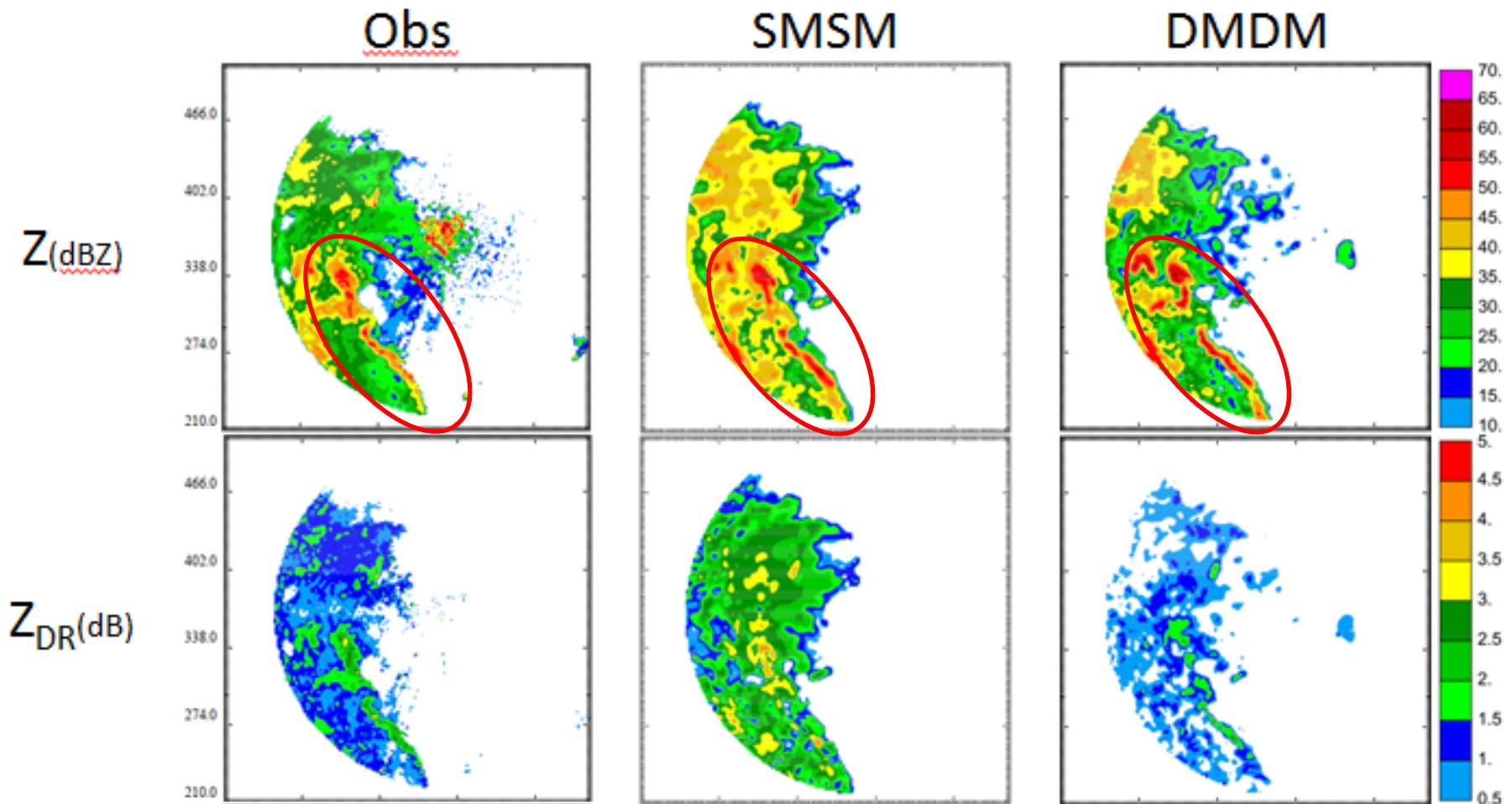


2-Hour Probabilistic Forecasts for Presence of Near-surface Vortices



# Single- and Dual-Moment Microphysical State Estimation With EnKF Direct Comparison with Radar Reflectivity

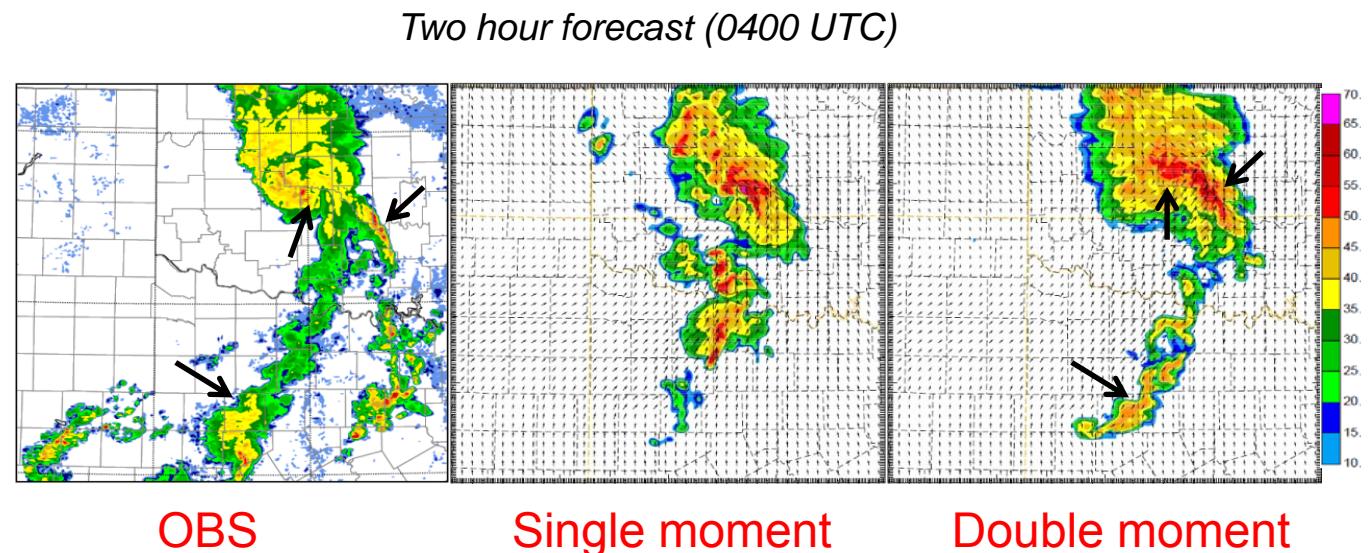
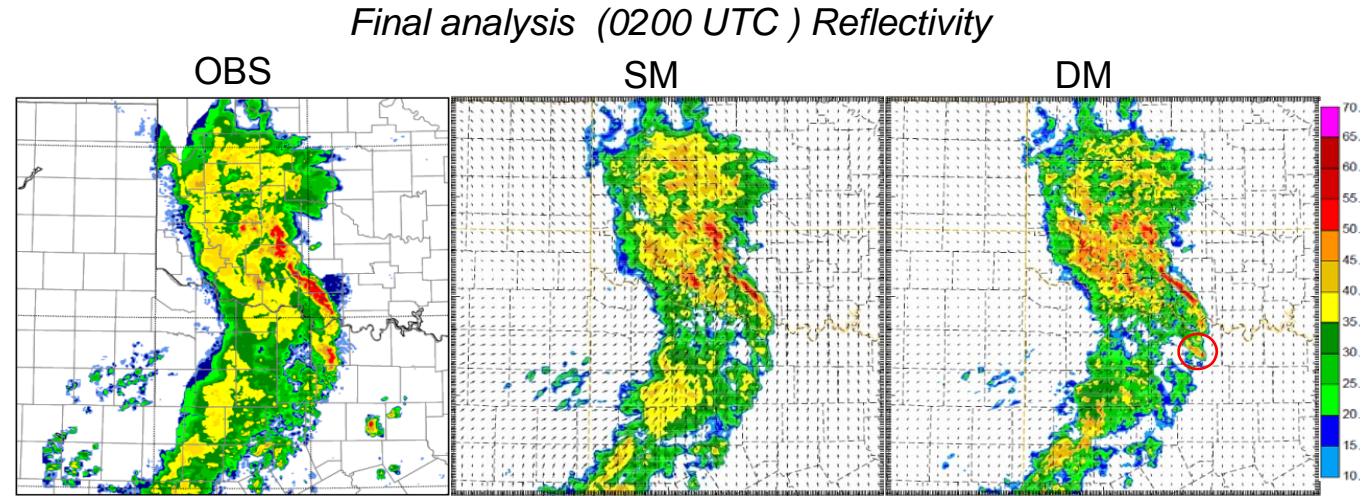
Simulated **dual-pol signatures** at the final analyses at 0.5 tilt



# Single- and Dual-Moment Microphysical State Estimation With EnKF

## Direct Comparison with Radar Reflectivity

- The analyzed reflectivity fields in both 1-moment and 2-moment experiments compare well with radar observations (shown at top).
- However, 2-moment forecast show significant improvement over the 1-moment experiment (shown at bottom).
- The structure and evolution of the forecast MCS, LEV and leading and trailing convective lines is remarkably better with a 2-moment scheme throughout the forecast period than with a 1-moment scheme.



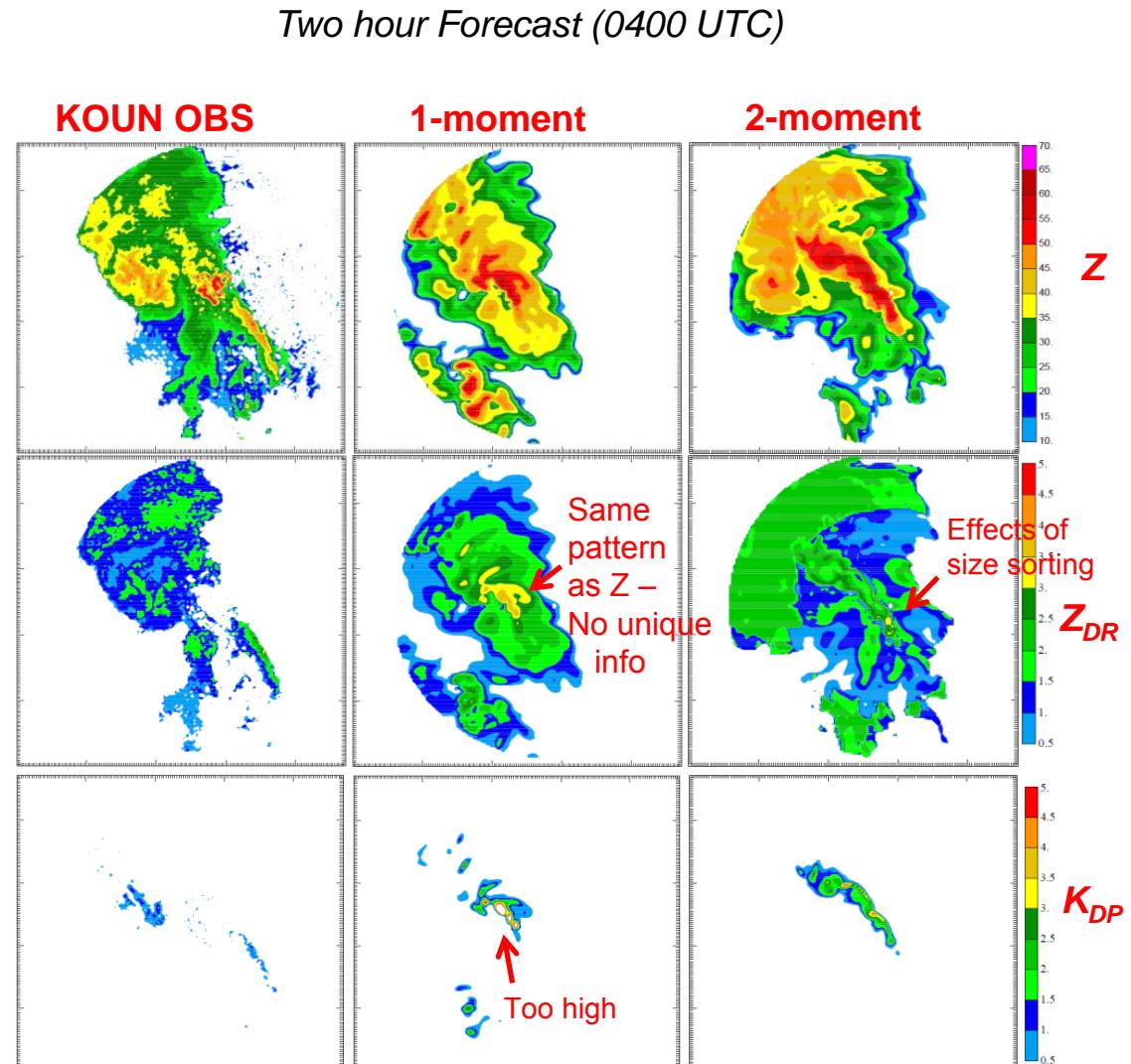
Poster 21.

# Single- and Dual-Moment Microphysical State Estimation With EnKF

## Direct Comparison with Polarimetric Variables

(Putnam, et al.)

- Polarimetric variables on .5 tilt as seen by KOUN using polarimetric radar data simulator (Jung et al. 2010)
- The polarimetric signatures are more realistic in the 2-moment results in general.
- Specifically, there is evidence of size sorting of hydrometeors on the leading edge of the system indicated by increased  $Z_{DR}$ . The reduction of  $Z_{DR}$  in the center of the line in 2-moment experiment is due to hail while observations show no sign of hail.
- $K_{DP}$  is unrealistically high in the 1-moment scheme (maximum  $\sim 11$  deg/km), suggesting an excess of rain drops. As with  $Z_{DR}$ , the 2-moment scheme values are also higher than observed, but the results are in a closer agreement with observations.

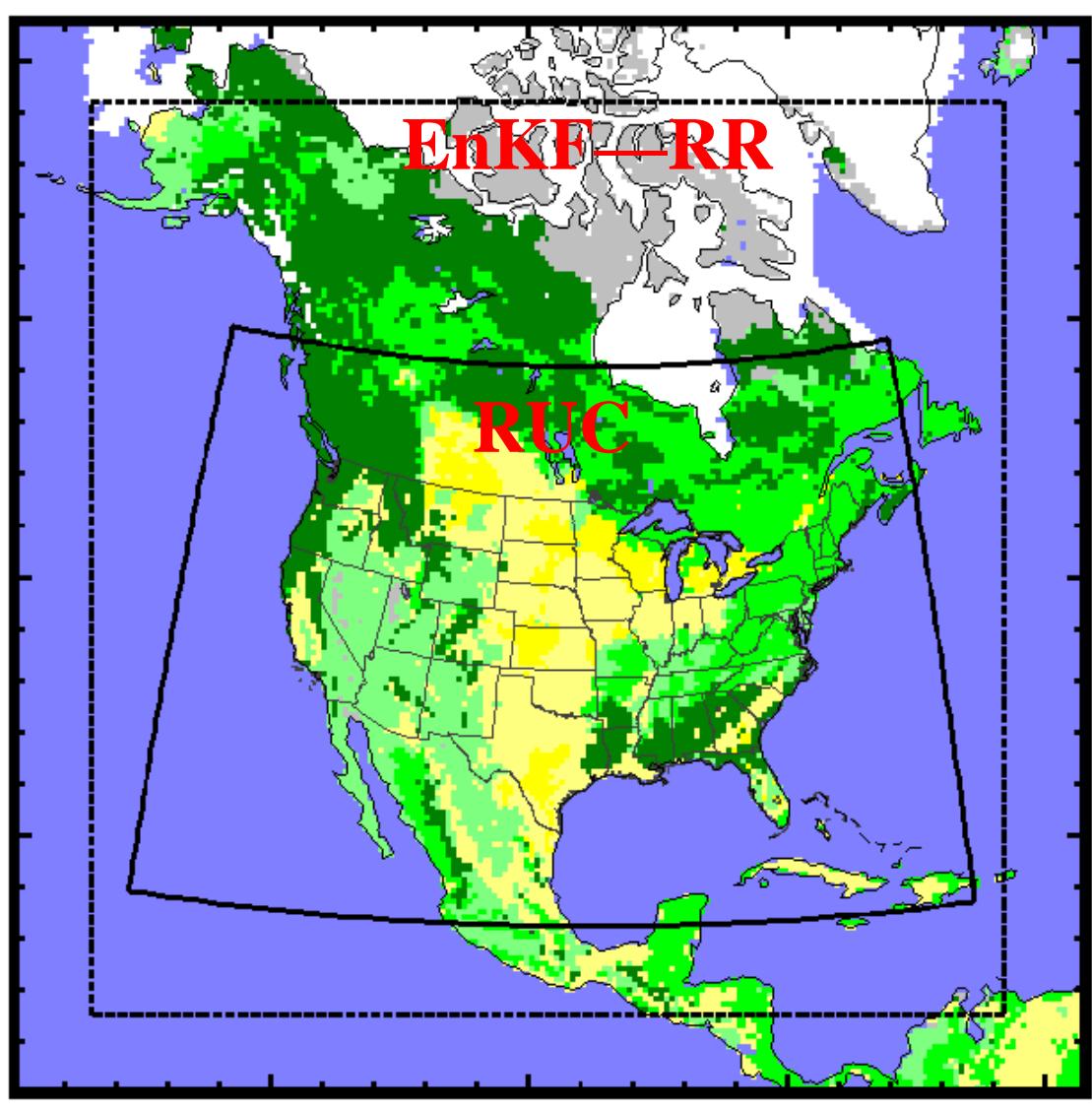


# Development and Testing of GSI-based EnKF and EnKF-Hybrid for Rapid Refresh Configurations

Kefeng Zhu, Yejie Pan, Ming Xue, Xuguang Wang  
Center for Analysis and Prediction of Storm

Jeffrey Whitaker, Stephen Weygandt, Stanley Benjamin, Ming Hu  
NOAA/ESRL

# FAA-Supported EnKF/Hybrid work for RR



## EnKF Test Domain

207x207 grid points  
~40 km, 51 levels

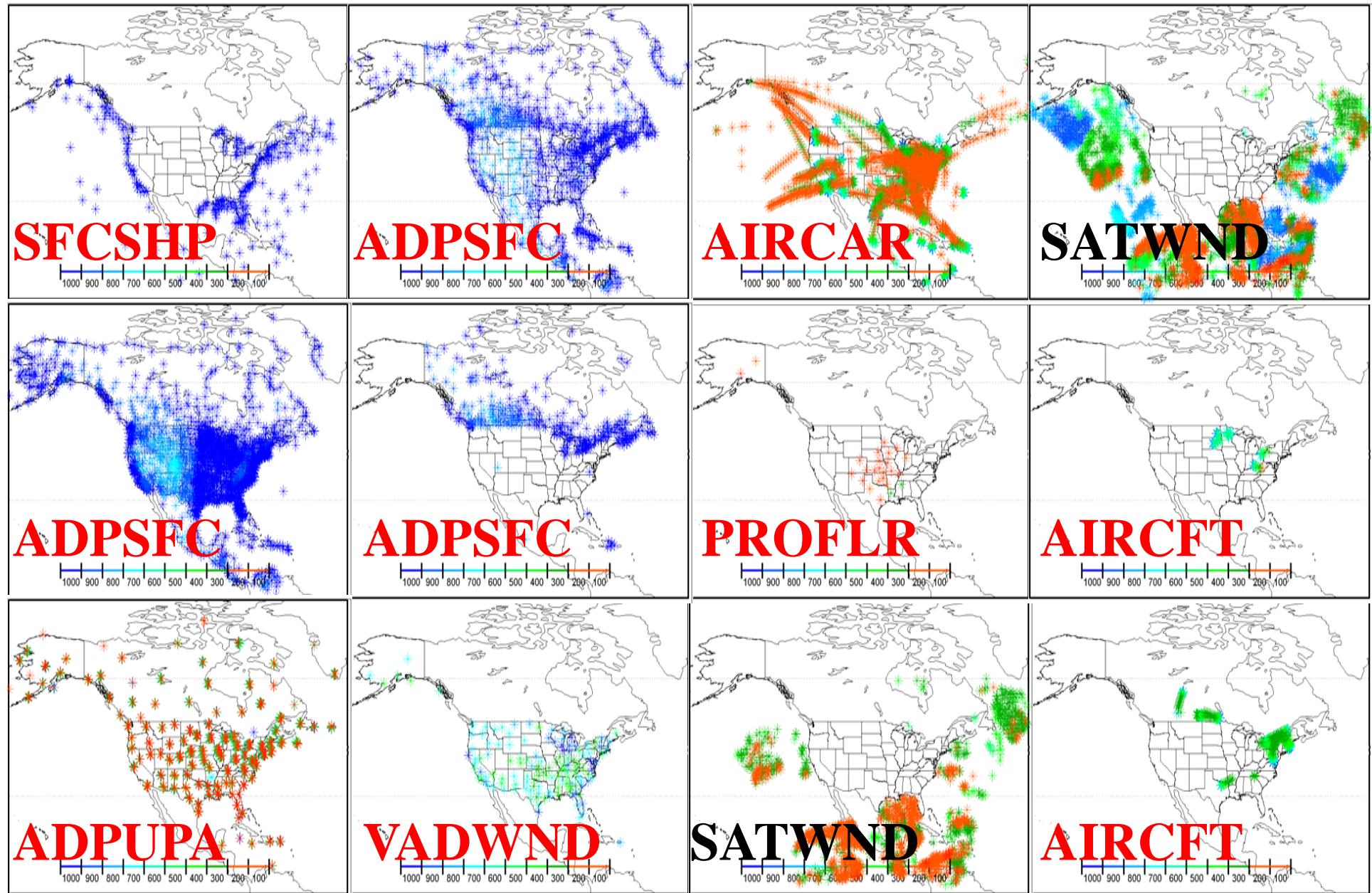
## The 13 km RR-like forecast Domain

532x532 grid points  
~13 km, 51 levels

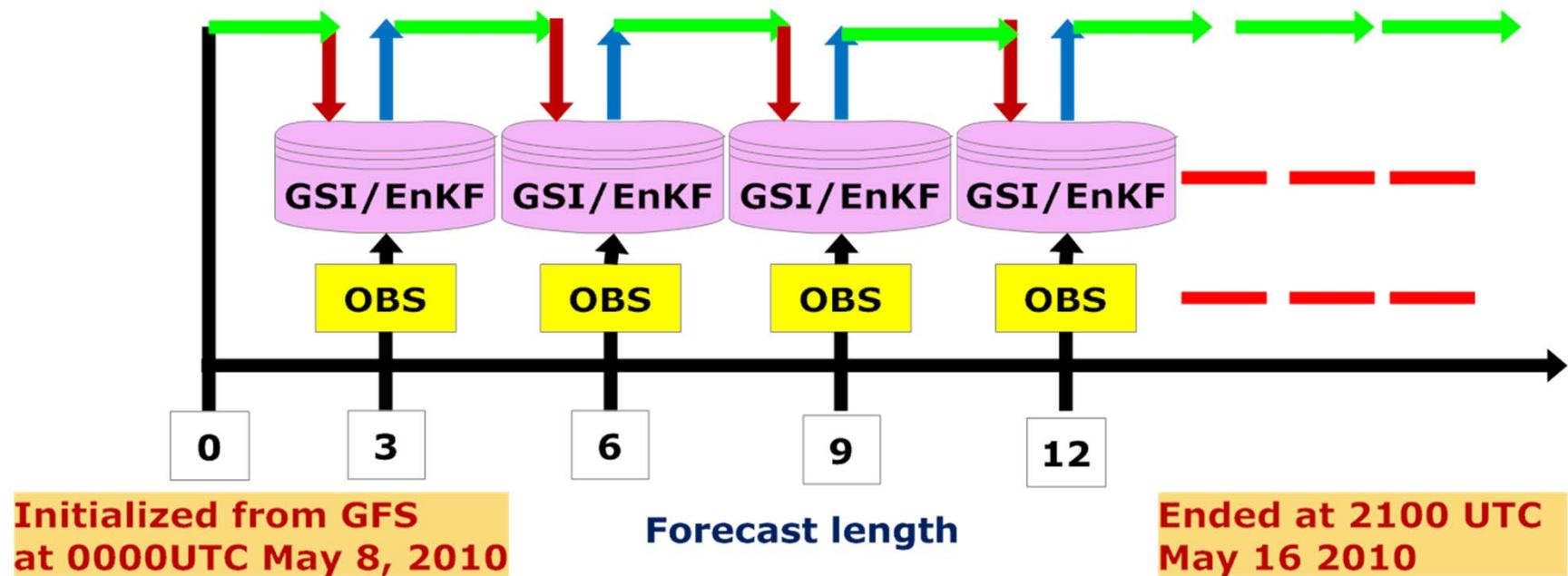
## Current RUC Domain as indicated

Started working on GSI-based hybrid

# Observation Distribution Valid at 2010051412

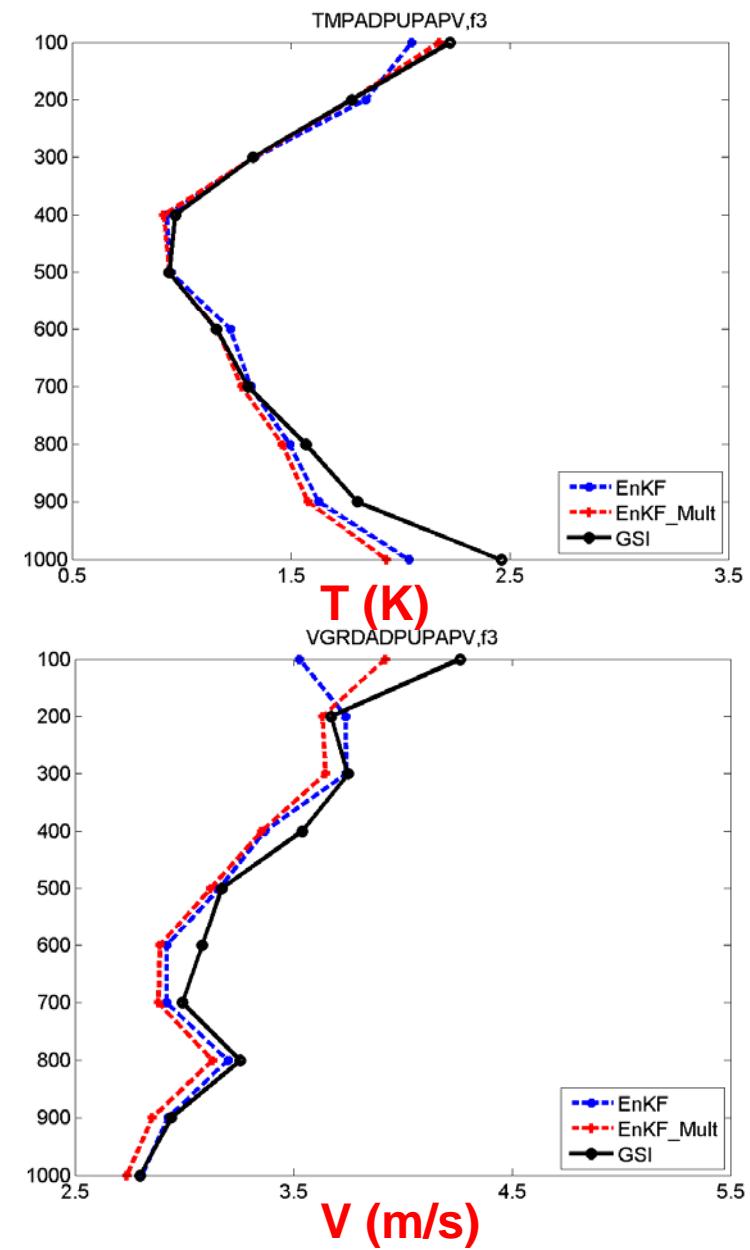
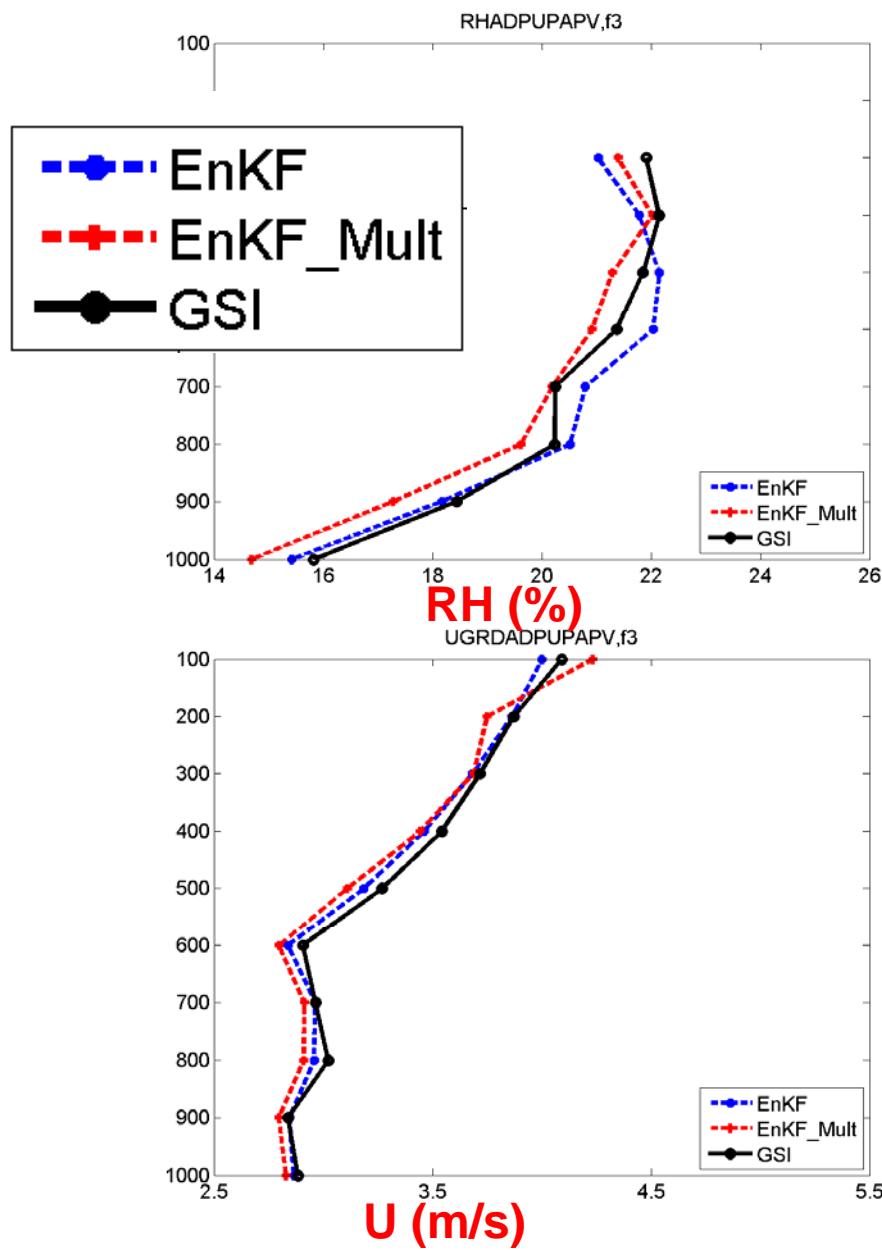


# Flowchart of EnKF/GSI

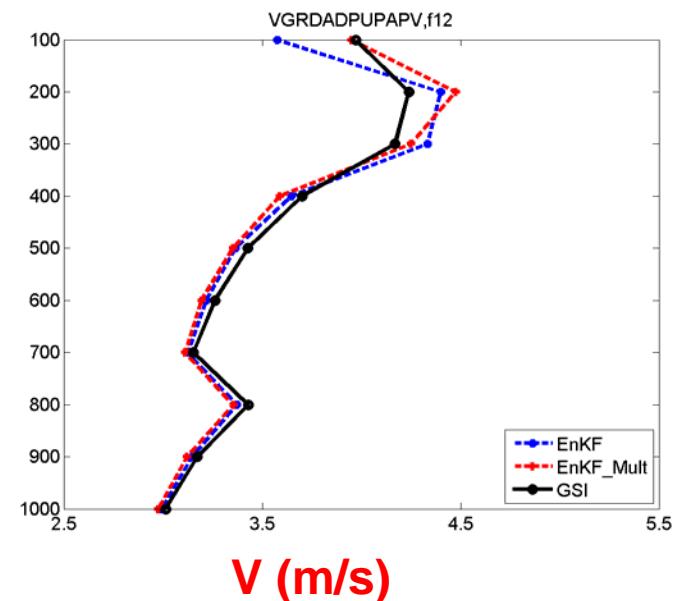
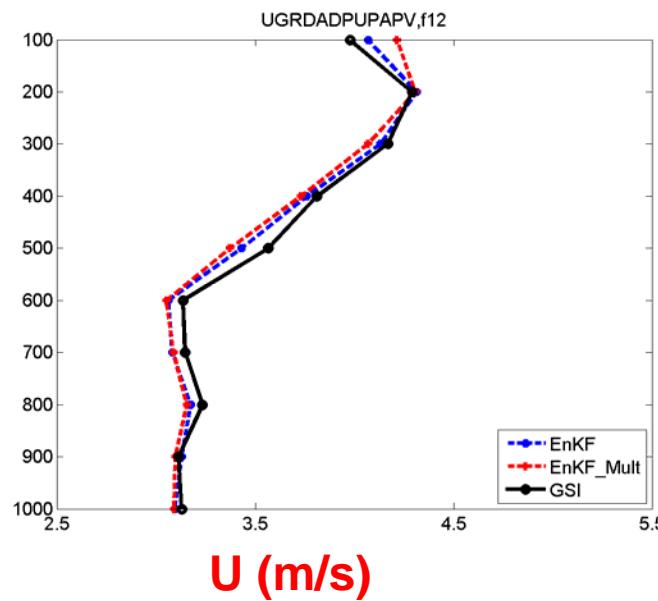
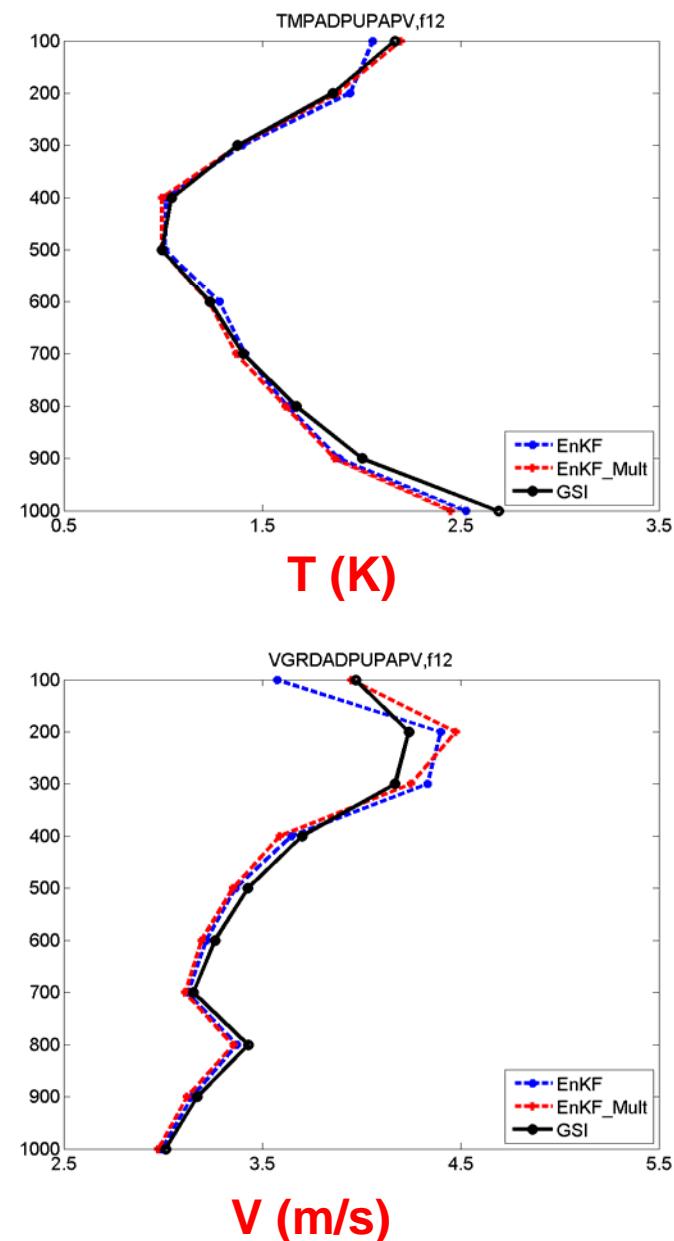
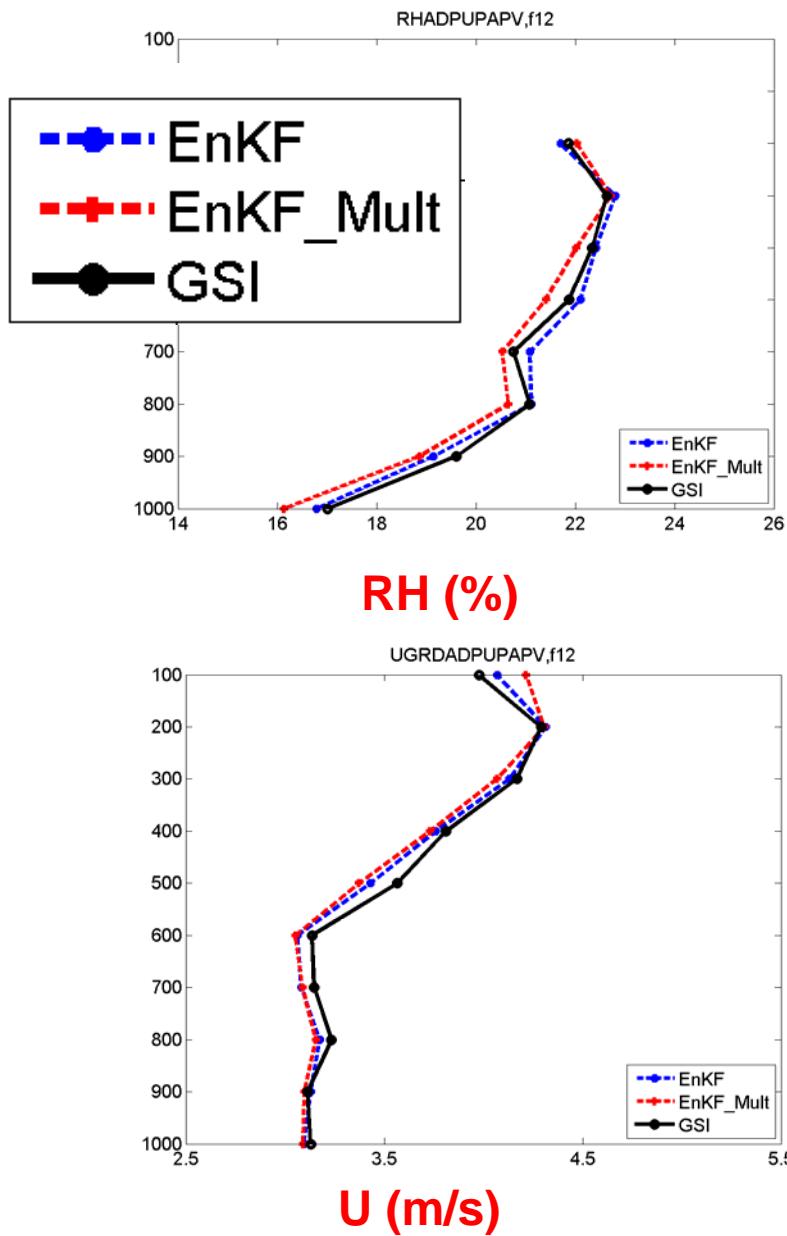


Both EnKF and GSI were run with 3-hourly assimilation cycles for a one-week-long test period starting at 00 UTC, May 8 2010.

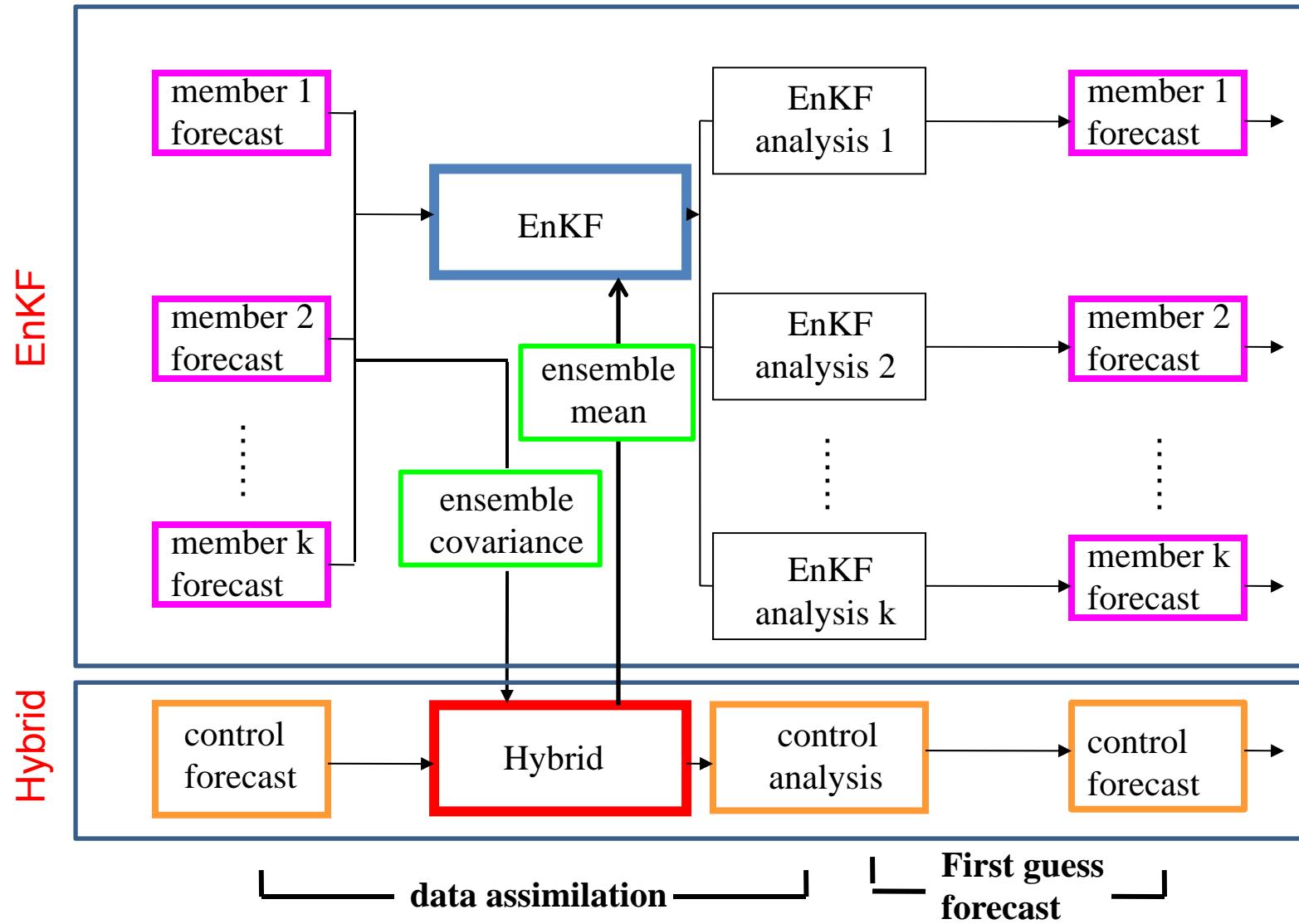
# 3-h forecasts verified against sounding (EnKF v.s. GSI)



# 12-h forecasts verified against sounding (EnKF v.s. GSI)



# EnKF-Hybrid DA System



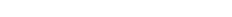
# How to incorporate ensemble in GSI?

- Ensemble covariance is included in the VAR cost function through augmentation of control variables (Lorenc 2003; Buehner 2005; Wang et al. 2007a, 2008a, Wang 2010) .
- Hybrid formula (Wang 2010 -- formula for GSI with B preconditioning):

$$\begin{aligned} J(\mathbf{x}_1^*, \mathbf{a}) &= \beta_1 J_1 + \beta_2 J_e + J_o \\ &= \beta_1 \frac{1}{2} \mathbf{x}_1^{*T} \mathbf{B}^{-1} \mathbf{x}_1^* + \beta_2 \frac{1}{2} \mathbf{a}^T \mathbf{C}^{-1} \mathbf{a} + \frac{1}{2} (\mathbf{y}^{o'} - \mathbf{Hx}^*)^T \mathbf{R}^{-1} (\mathbf{y}^{o'} - \mathbf{Hx}^*) \end{aligned}$$

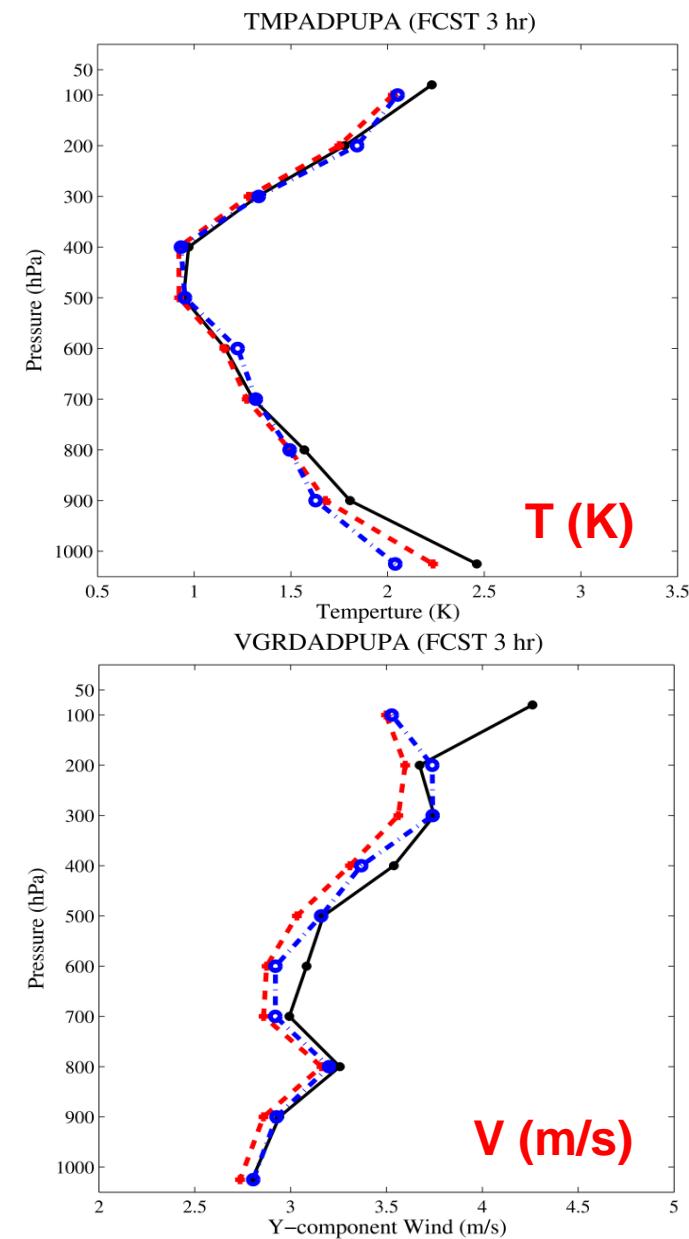
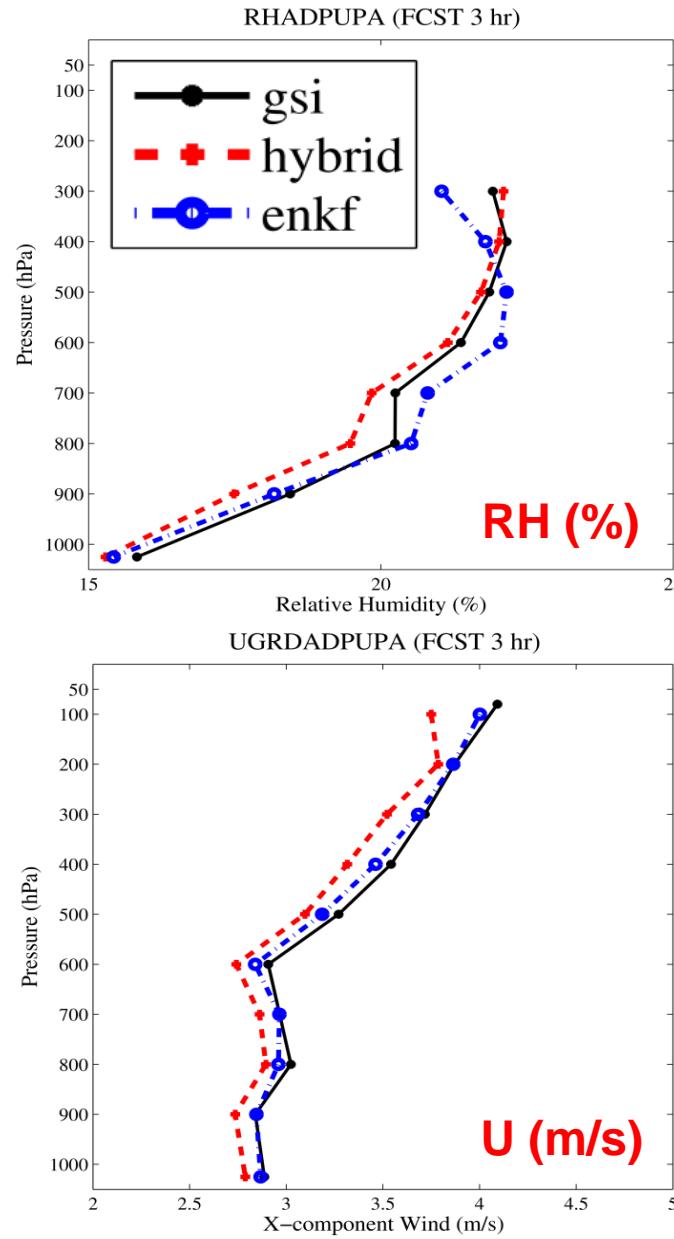
 Extra term associated with extended control variable

$$\mathbf{x}^* = \mathbf{x}_1^* + \sum_{k=1}^K (\mathbf{a}_k \circ \mathbf{x}_k^e)$$

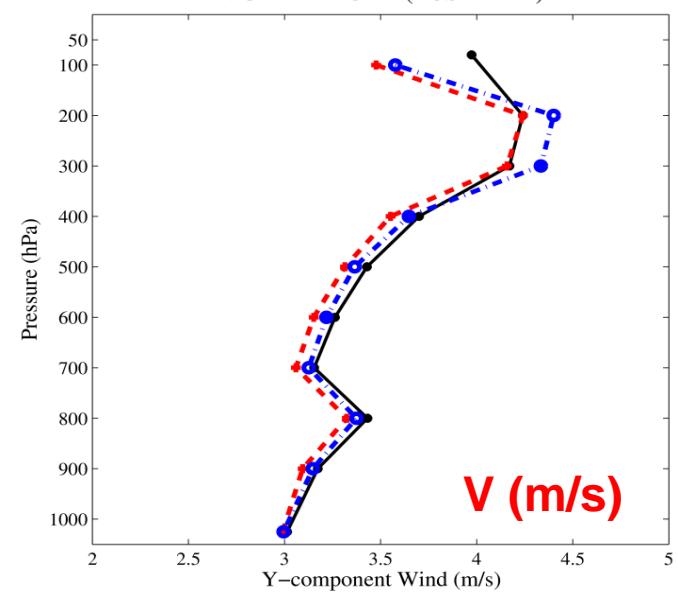
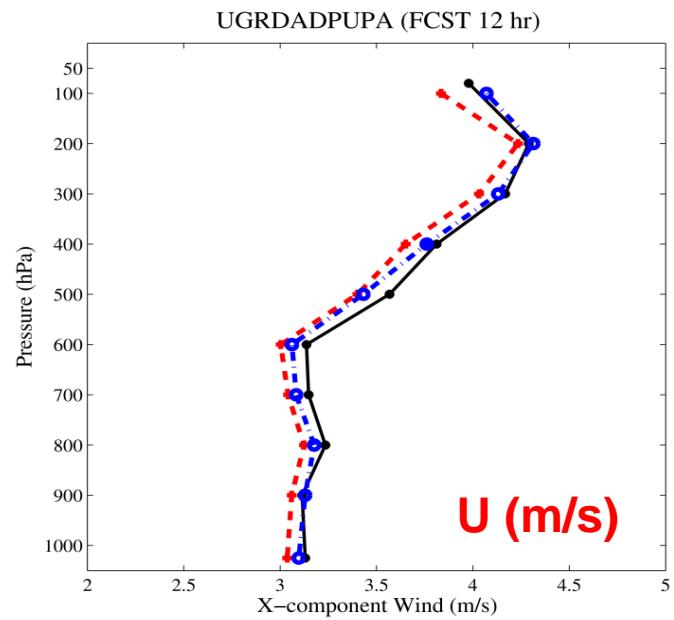
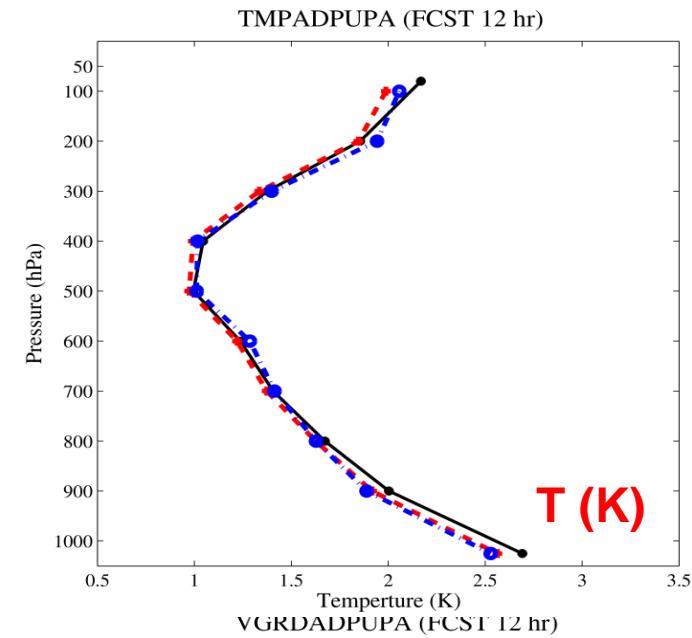
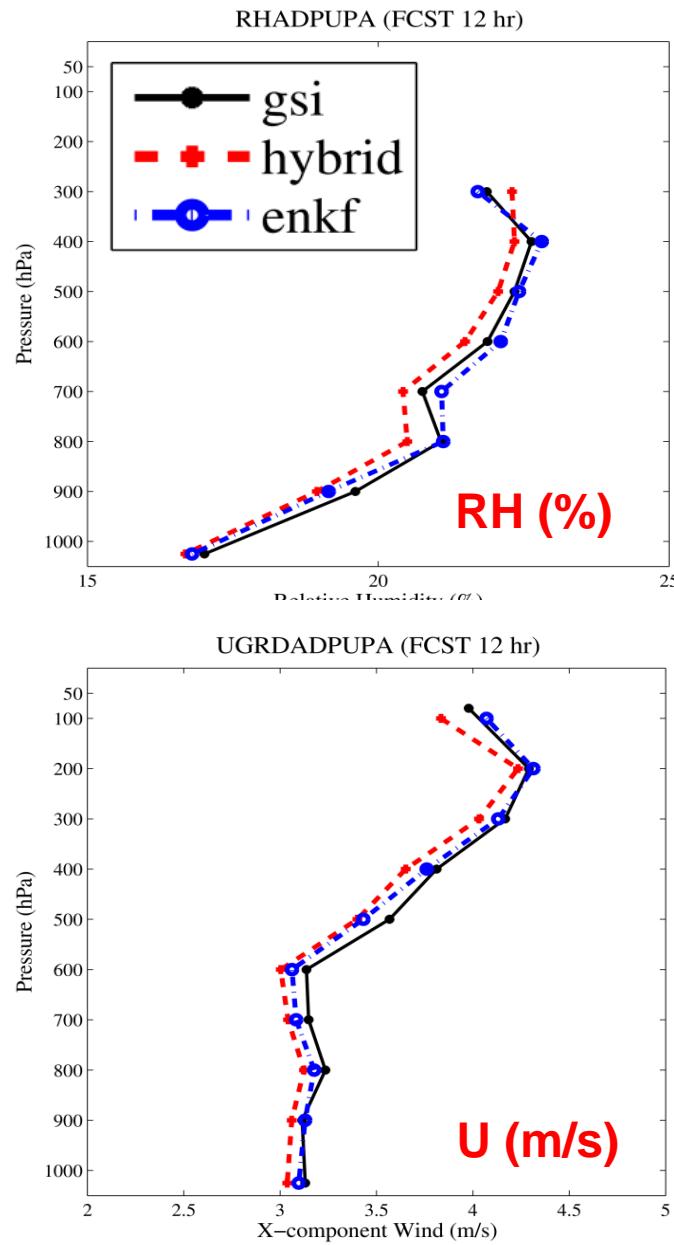
 Extra increment associated with ensemble

**B** 3DVAR static covariance; **R** observation error covariance; **K** ensemble size;  
**C** correlation matrix for ensemble covariance localization;  $\mathbf{x}_k^e$   $k$ th ensemble perturbation;  
 $\mathbf{x}_1^*$  3DVAR increment;  $\mathbf{x}^*$  total (hybrid) increment;  $\mathbf{y}^{o'}$  innovation vector;  
**H** linearized observation operator;  $\beta_1$  weighting coefficient for static covariance;  
 $\beta_2$  weighting coefficient for ensemble covariance; **a** extended control variable.

# 3-h fcsts verified against sounding (EnKF v.s. Hybrid v.s. GSI)

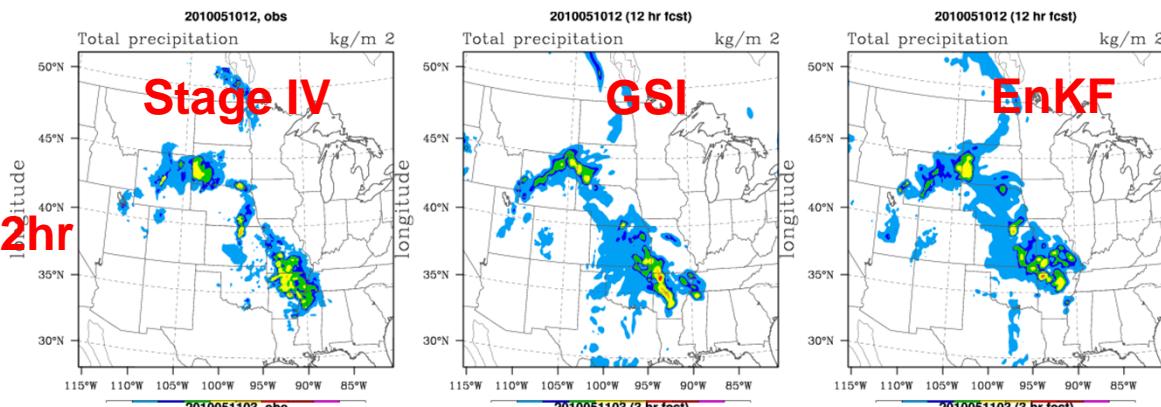


# 12-h fcsts verified against sounding (EnKF v.s. Hybrid v.s. GSI)

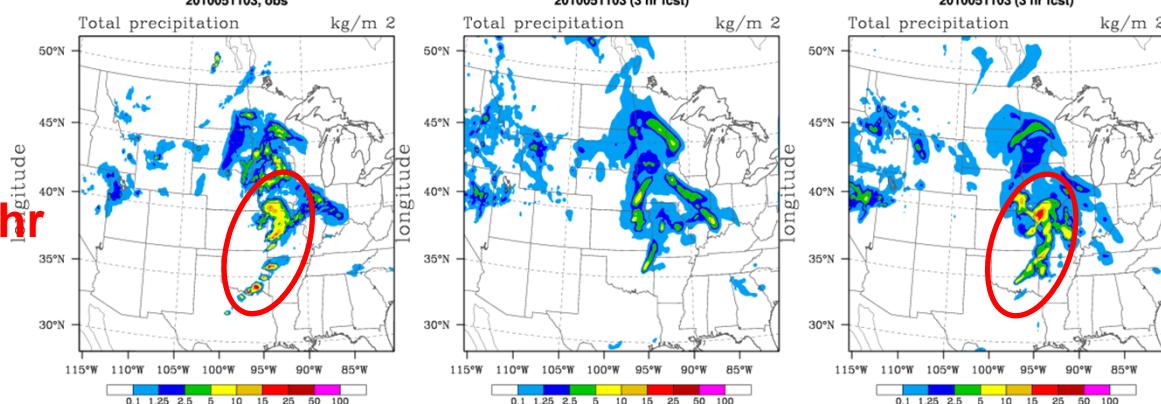


# 1 hour accumulated precipitation forecasts on 13 km grid

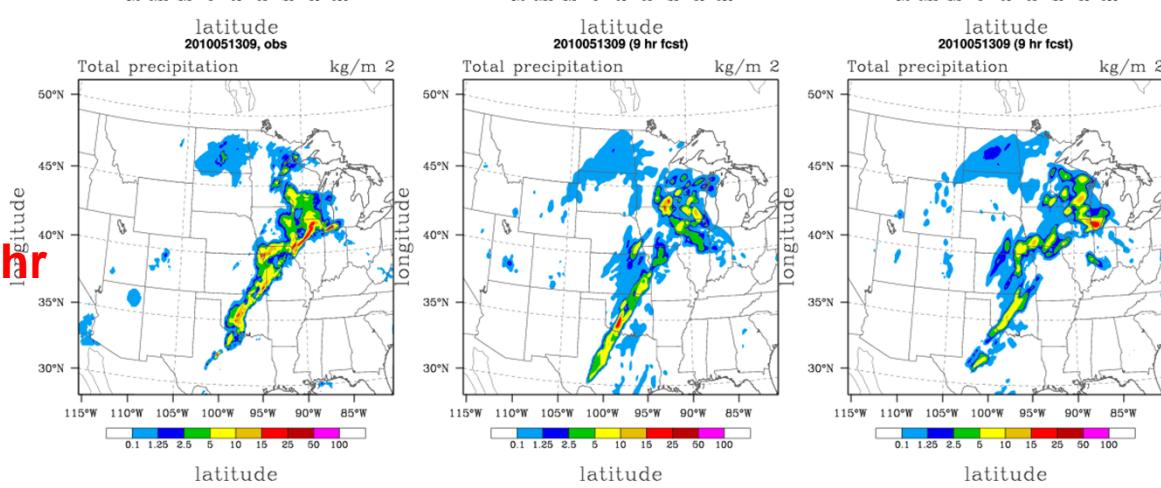
2010051000+12hr



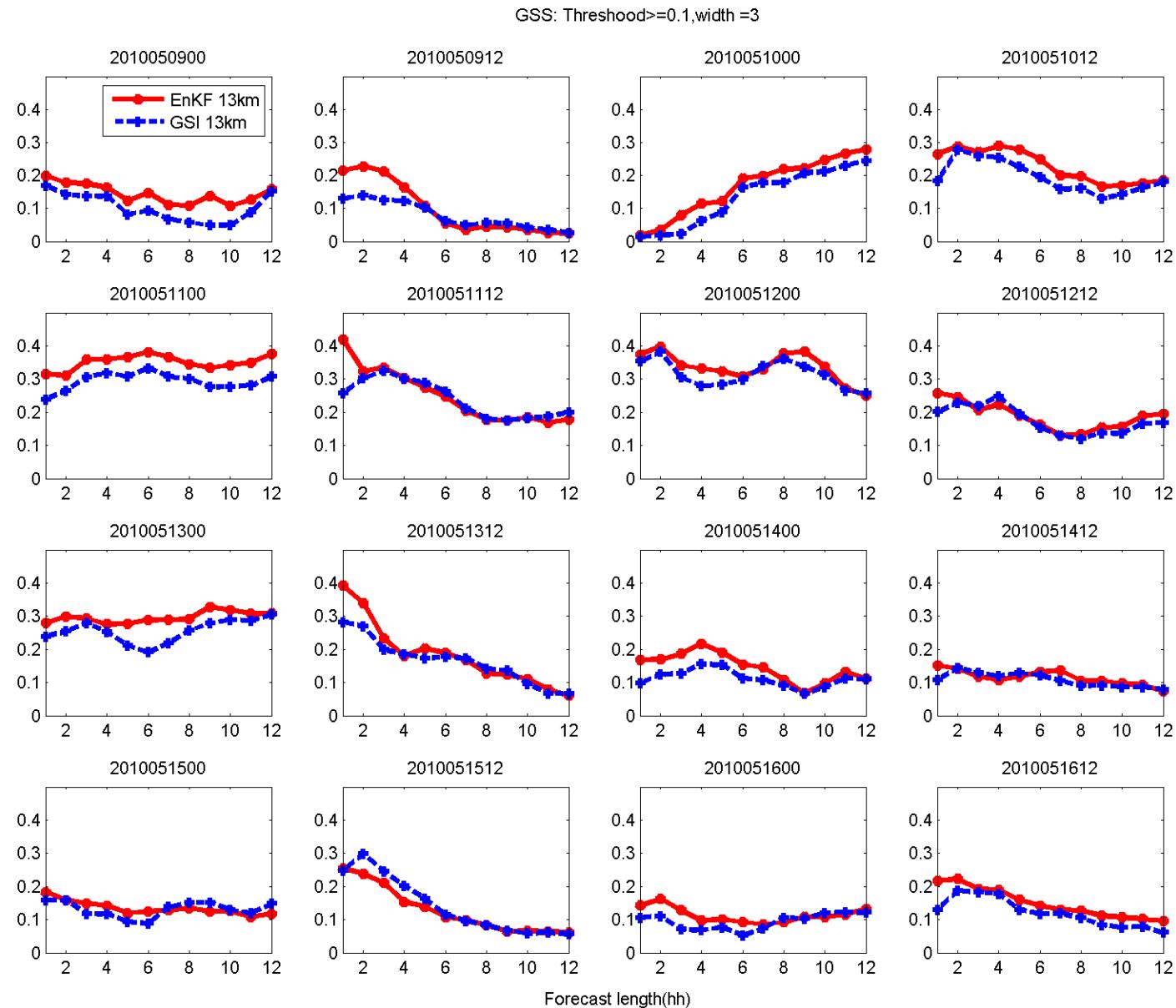
2010051100+3hr



2010051300+9hr

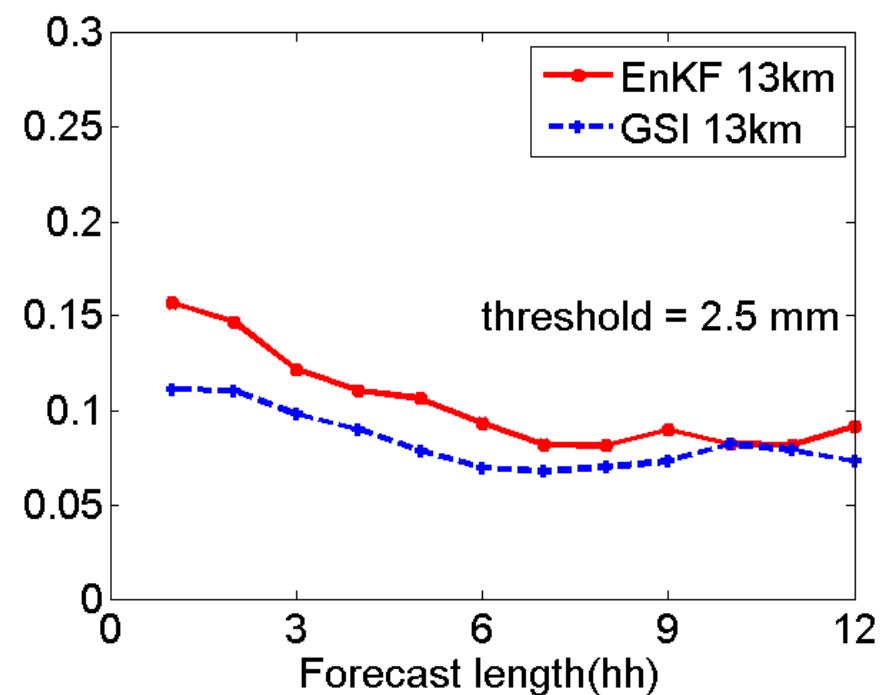
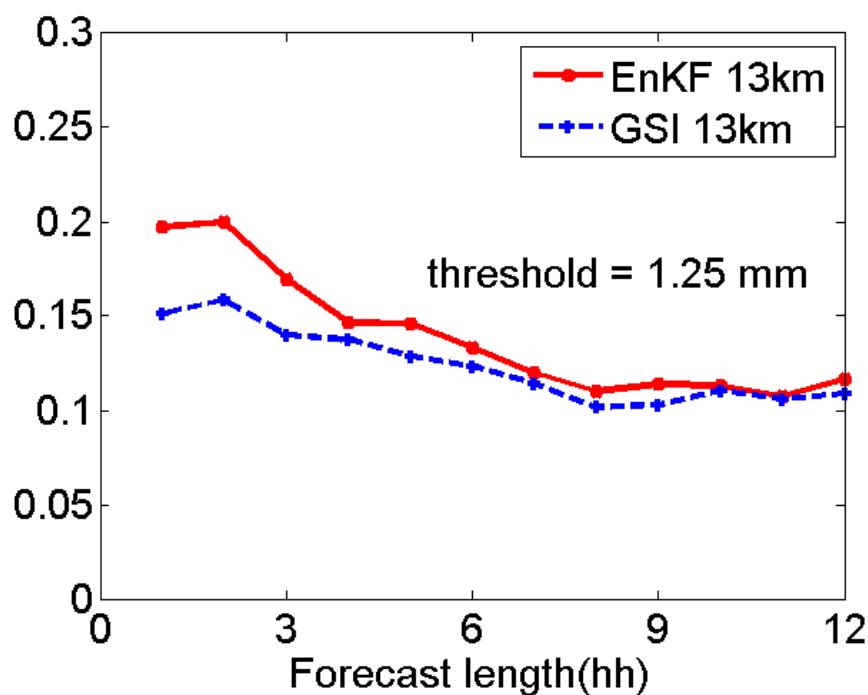
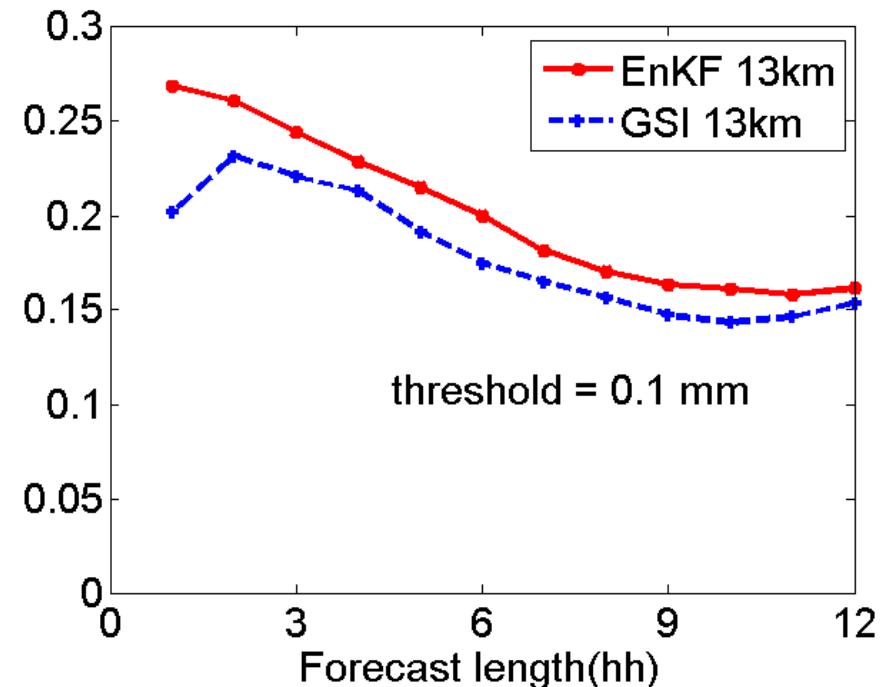


# 13 km hourly QPF verification (ETS scores)



**GSS/ETS, Threshold=0.1mm/h**

## Average GSS/ETS Scores for all forecasts

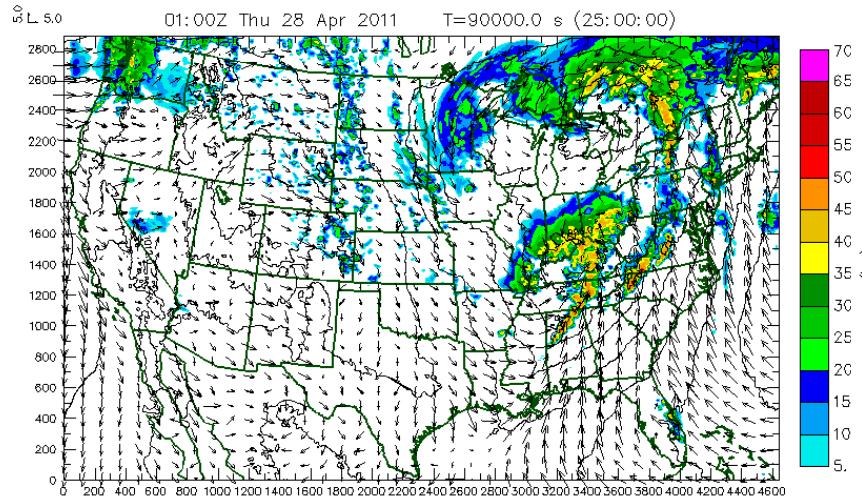


# Ambition for the next few years

- Central Great Plain ~4 km domain continuous EnKF cycles including all radar data in realtime, nesting inside RR EnKF/hybrid ensemble
- CONUS-domain ~4 km EnKF/hybrid cycles including all data (including satellite) used in Rapid Refresh GSI plus all radar data
- Sub-km cycled EnKF with 88D and CASA-type high-resolution radars.
- Use EnKF analyses to initialize convection-resolving ensemble probabilistic forecasting

# CAPS CRTM Simulation –Preliminary Results

## Composite Reflectivity



25-h 4 km WRF forecast with WSM6  
01 UTC, April 28, 2011

From  
Jason  
Otkin  
ABI  
8.5  $\mu$ m

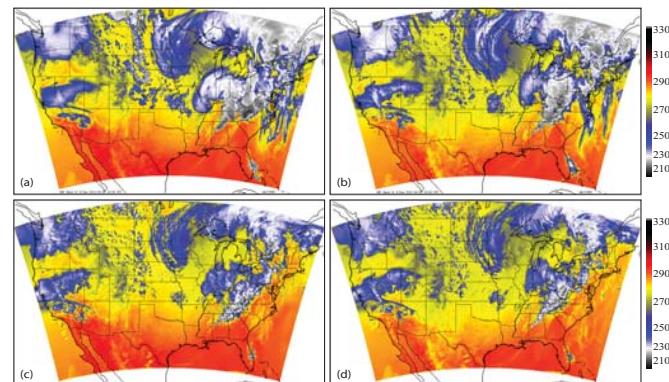


Fig. 1. Simulated ABI 8.5  $\mu$ m brightness temperatures (K) valid at 0100 UTC on 28 April 2011 for four CAPS ensemble members.

## 8.5 $\mu$ m

